

Influence of the spin-phonon interaction on the tunneling gap of single-molecule magnets

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"HIGH-SPIN MOLECULES AND MOLECULAR MAGNETS"
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Questions for today



$$\begin{pmatrix} 3 & 42 & 4711 \\ 42 & 0 & 3.14 \\ 4711 & 3.14 & 8 \\ -17 & 007 & 13 \\ 1.8 & 15 & 081 \end{pmatrix}$$

1. Can the spin-phonon interaction open a tunneling gap?
2. Are there innocent phonons due to symmetry?

We are the sledgehammer team of matrix diagonalization.
Please send inquiries to [jschnack@uni-bielefeld.de!](mailto:jschnack@uni-bielefeld.de)

Model Hamiltonian (effective, spin-only, bilinear)

$$\tilde{H} = \sum_{i,j} \vec{s}(i) \cdot \mathbf{J}_{ij} \cdot \vec{s}(j) + \mu_B \vec{B} \cdot \sum_i^N \mathbf{g}_i \cdot \vec{s}(i)$$

Exchange/Anisotropy Zeeman

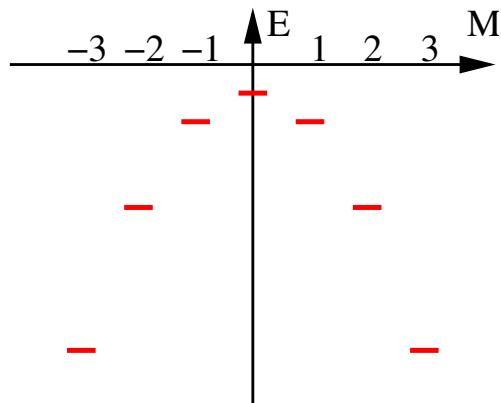
\mathbf{J}_{ij} : Heisenberg exchange, anisotropic exchange, and single-ion anisotropy.

Isotropic Heisenberg Hamiltonian

$$\tilde{H} = -2 \sum_{i < j} J_{ij} \vec{s}(i) \cdot \vec{s}(j) + g \mu_B B \sum_i^N s_z(i)$$

Heisenberg Zeeman

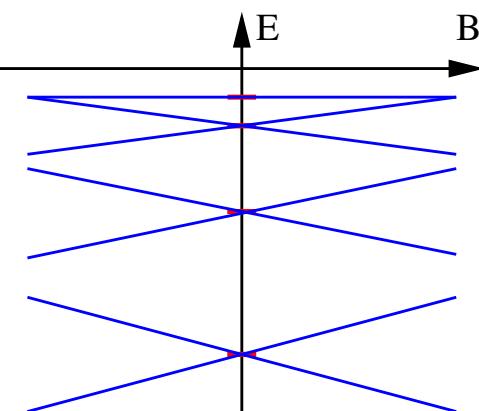
Single-ion anisotropy – single spin I



$$\tilde{H} = D(\tilde{s}^z)^2 + g\mu_B B \tilde{s}^z$$

$D < 0$ easy axis, $D > 0$ hard axis;

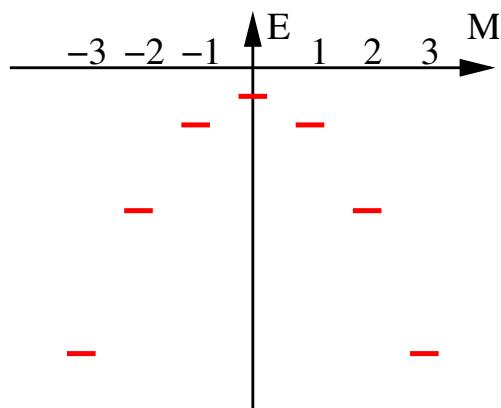
eigenvectors: $|s, m\rangle$



eigenvalues: $E_m = Dm^2 + g\mu_B B m$, $m = -s, \dots, s$

IMPORTANT: $[\tilde{H}, \tilde{s}^z] = 0 \Rightarrow$ level crossings at $B = 0$

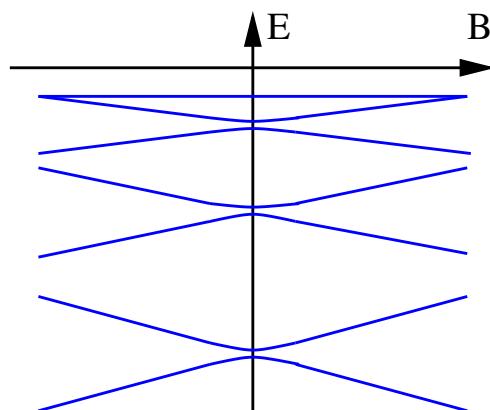
Single-ion anisotropy – single spin II



$$\tilde{H} = D(\tilde{s}^z)^2 + E \left\{ (\tilde{s}^x)^2 - (\tilde{s}^y)^2 \right\} + g\mu_B B \tilde{s}^z$$

$|E| < |D|$ – major axes of the anisotropy tensor;

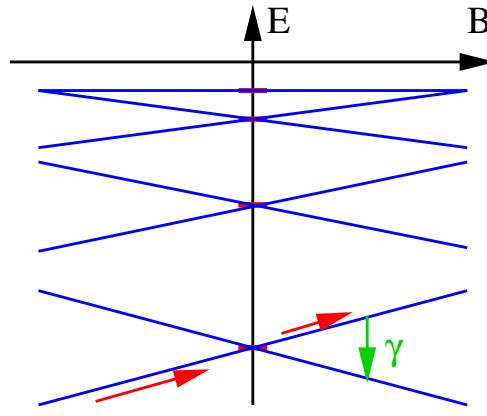
NO LONGER eigenvectors: $|s, m\rangle$



eigenvalues are more complicated functions of $\vec{B} = B\vec{e}_z$: $E_\mu(B)$

IMPORTANT: $[H, \tilde{s}^z] \neq 0 \Rightarrow$ avoided level crossings at $B = 0$ for integer spins
(otherwise Kramers degeneracy)

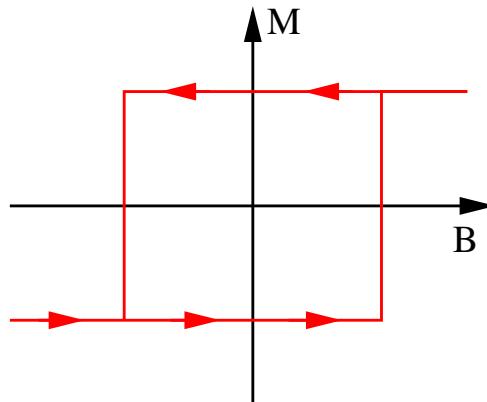
Bistability – uniaxial system – S^z -symmetry



Goal: single-molecule magnets (SMM)

$$\tilde{H} = \sum_i D_i(\tilde{s}_i^z)^2 + \mu_B B \sum_i g_i \tilde{s}_i^z + H_{\text{ferro int}}$$

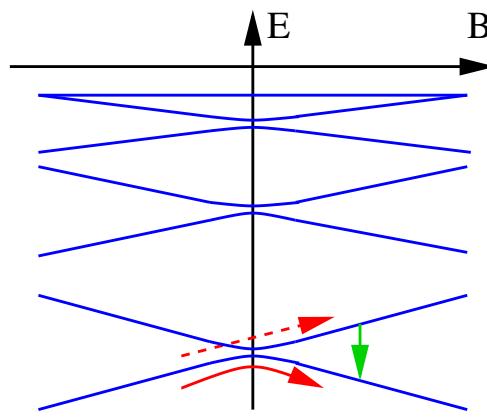
IMPORTANT: $[\tilde{H}, \tilde{S}^z] = 0 \Rightarrow$ level crossings at $B = 0$



⇒ low-temperature TIME-DEPENDENT hysteresis

Side remark: For macroscopic systems in the ferromagnetic phase the relaxation time is HUGE, that's why we don't experience it.

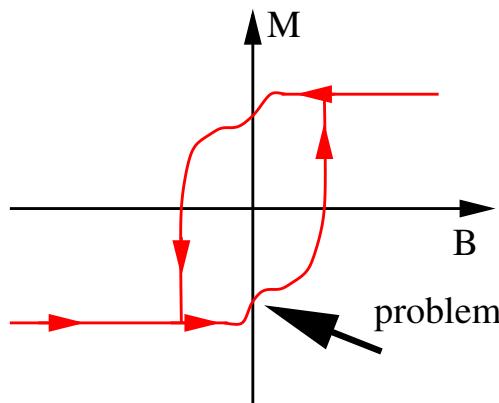
Bistability – general system – NO \tilde{S}^z -symmetry



$$\tilde{H} = \sum_i \vec{s}_i \cdot \mathbf{D}_i \cdot \vec{s}_i + \mu_B B \sum_i g_i s_i^z + H_{\text{ferro int}}$$

\mathbf{D}_i individual anisotropy tensors

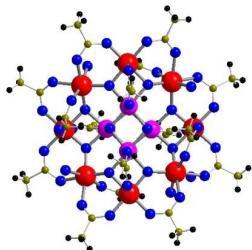
⇒ low-temperature TIME-DEPENDENT hysteresis closes at $B = 0$ – not bistable & bad for storage



REASON: branching at avoided level crossings;
strong dependence on tunneling gap and \dot{B} ;

slow change of $B \Rightarrow$ system follows ground state,
compare Landau-Zener-Stückelberg
or slow/fast train at switch

Bistability – state of the art

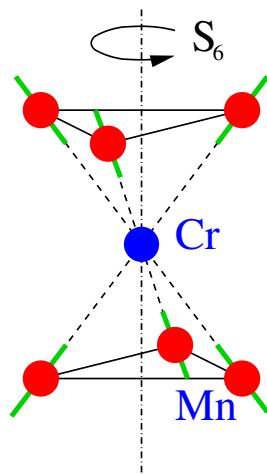


Today's major goals:

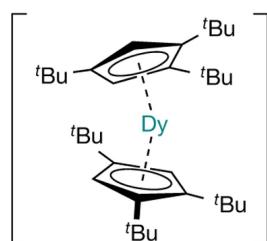
ferromagnetic spin-spin interaction

uniaxial anisotropy tensors

symmetry that does not permit E -terms



PERSISTENT PROBLEM: phonons



Nick Chilton, Thorsten Glaser, Jeff Long, Alessandro Lunghi, Mark Murrie, Frank Neese, Stefano Sanvito, Roberta Sessoli, Richard Winpenny, Yan-Zhen Zheng, ...

Can spin-phonon interaction induce a tunneling gap?

Spin-phonon interaction – DFT view of the problem

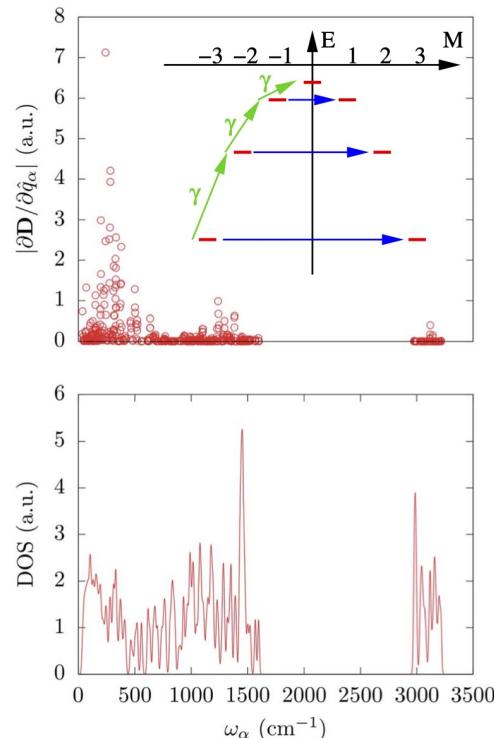


Fig. 2 Top panel: calculated spin-phonon coupling coefficients projected onto the normal modes basis set and displayed as a function of the modes frequency. Bottom panel: DFT calculated density of states for the T -point normal modes of vibration.

Calculate structure by means of DFT (1)

Calculate phonon density of states by means of DFT + molecular dynamics (1,2,3)

Calculate coupling coefficients from DFT (2,3,4)

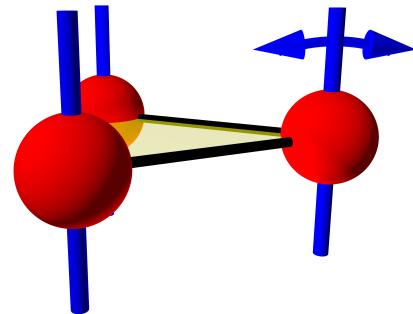
Perturbation picture: set up rate equations for phonon transitions between eigenstates of unperturbed spin Hamiltonian (2,3)

ADVANTAGE: many realistic phonons

- (1) A. V. Postnikov, J. Kortus, and M. R. Pederson, *physica status solidi (b)* **243**, 2533 (2006).
- (2) A. Lunghi and S. Sanvito, *Science Advances* **5**, eaax7163 (2019).
- (3) A. Albino, S. Benci, L. Tesi, M. Atzori, R. Torre, S. Sanvito, R. Sessoli, and A. Lunghi, *Inorg. Chem.* **58**, 10260 (2019);
⇒ figure.
- (4) D.A.S. Kaib, S. Biswas, K. Riedl, S.M. Winter, R. Valentí, *Phys. Rev. B* **103**, L140402 (2021).

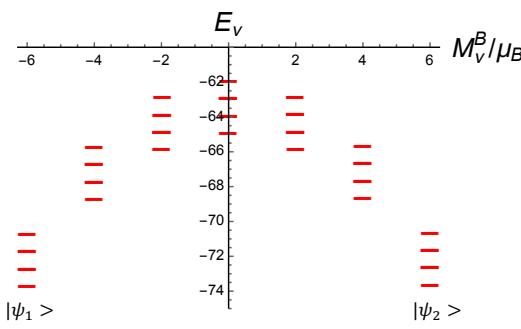
Spin-phonon interaction – our question

Can phonons induce a tunnel splitting?



Know that non-collinear easy axes produce tunnel splitting

Set up special phonon modes that tilt easy axes in plane with C_3 axis out of uniaxial alignment



ADVANTAGE: quantum many-body solution for spins and phonons

⇒ correlated spin-phonon states:

$$|\Psi_\nu\rangle = \sum c_{m_1, m_2, m_3, n_1, n_2, n_3}^\nu |m_1, m_2, m_3, n_1, n_2, n_3\rangle$$

(1) K. Irländer and J. Schnack, Phys. Rev. B **102**, 054407 (2020).

Spin-phonon interaction – Hamiltonian

$$\begin{aligned}
 \tilde{H} = & -2J \left(\vec{s}_{\sim 1} \cdot \vec{s}_{\sim 2} + \vec{s}_{\sim 2} \cdot \vec{s}_{\sim 3} + \vec{s}_{\sim 3} \cdot \vec{s}_{\sim 1} \right) \\
 & + \vec{s}_{\sim 1} \cdot \mathbf{D}_1(\theta_1) \cdot \vec{s}_{\sim 1} + \vec{s}_{\sim 2} \cdot \mathbf{D}_2(\theta_2) \cdot \vec{s}_{\sim 2} + \vec{s}_{\sim 3} \cdot \mathbf{D}_3(\theta_3) \cdot \vec{s}_{\sim 3} \\
 & + \omega_1 \left(\tilde{a}_{\sim 1}^\dagger \tilde{a}_{\sim 1} + \frac{1}{2} \right) + \omega_2 \left(\tilde{a}_{\sim 2}^\dagger \tilde{a}_{\sim 2} + \frac{1}{2} \right) + \omega_3 \left(\tilde{a}_{\sim 3}^\dagger \tilde{a}_{\sim 3} + \frac{1}{2} \right) \\
 & + g\mu_B \cdot \vec{B} \cdot \left(\vec{s}_{\sim 1} + \vec{s}_{\sim 2} + \vec{s}_{\sim 3} \right)
 \end{aligned}$$

$$\mathbf{D}_i(\theta_i) = D \vec{e}_i(\theta_i, \phi_i) \otimes \vec{e}_i(\theta_i, \phi_i)$$

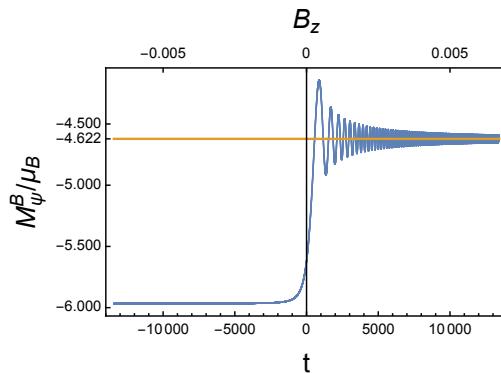
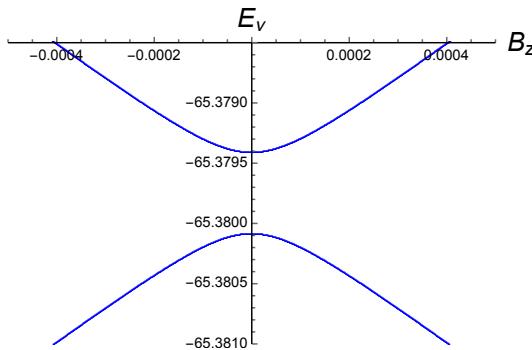
$$\tilde{\theta}_i = \theta_{i,0} + \alpha \left(\tilde{a}_i^\dagger + \tilde{a}_i \right), \quad \theta_{i,0} = 0, \quad \text{i.e., zero mean tilt}$$

Spin-phonon interaction – our result (applies to integer spins)

Can phonons induce a tunnel splitting?

⇒ Yes, they can!

Ground state, practically, does not contain any phonons, nevertheless tunneling occurs. Coupling to zero-point motion suffices (2).



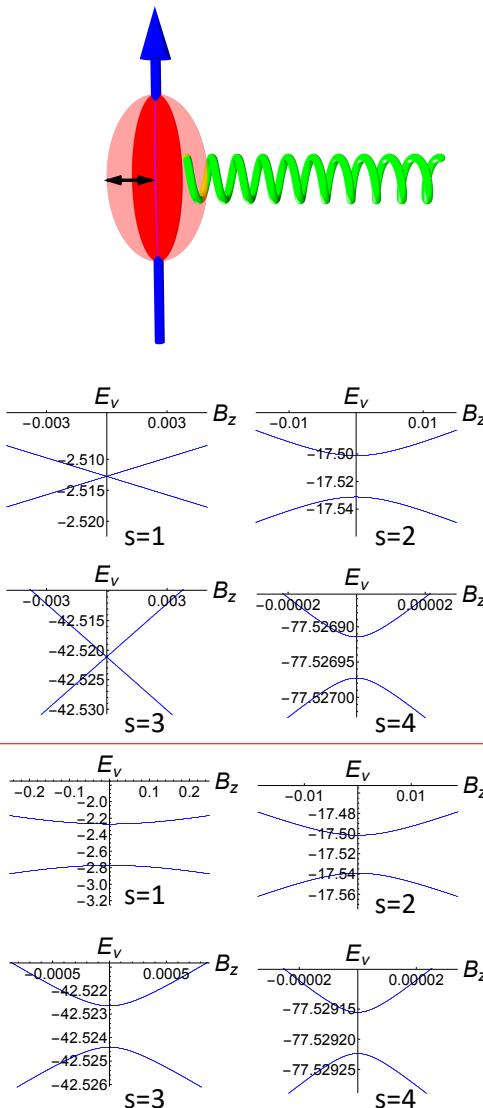
BAD NEWS: It is not enough to cool quantum devices, you have to prevent the coupling to disturbing sources at all.

Side remark: result probably already known in field of vibronic coupling (Atanasov, Shrivastava, Tsukerblat, Coronado).

- (1) K. Irländer and J. Schnack, Phys. Rev. B **102**, 054407 (2020).
- (2) F. Ortú *et al.*, Dalton Trans. **48**, 8541 (2019).

Innocent spin-phonon interaction due to symmetry

SUSY spin-phonon interaction (applies to integer spins)



$$\tilde{H} = D(\tilde{s}^z)^2 + E \left\{ (\tilde{s}^x)^2 - (\tilde{s}^y)^2 \right\} + g\mu_B B \tilde{s}^z + \tilde{H}_{\text{HO}}$$

Special phonons that modify only:

$$\text{L: } E = \alpha \left(\tilde{a}^\dagger + \tilde{a} \right) \quad \text{or} \quad \text{Q: } E = \alpha \left(\tilde{a}^\dagger + \tilde{a} \right)^2$$

L: tunneling gap for even s , no gap for odd s .

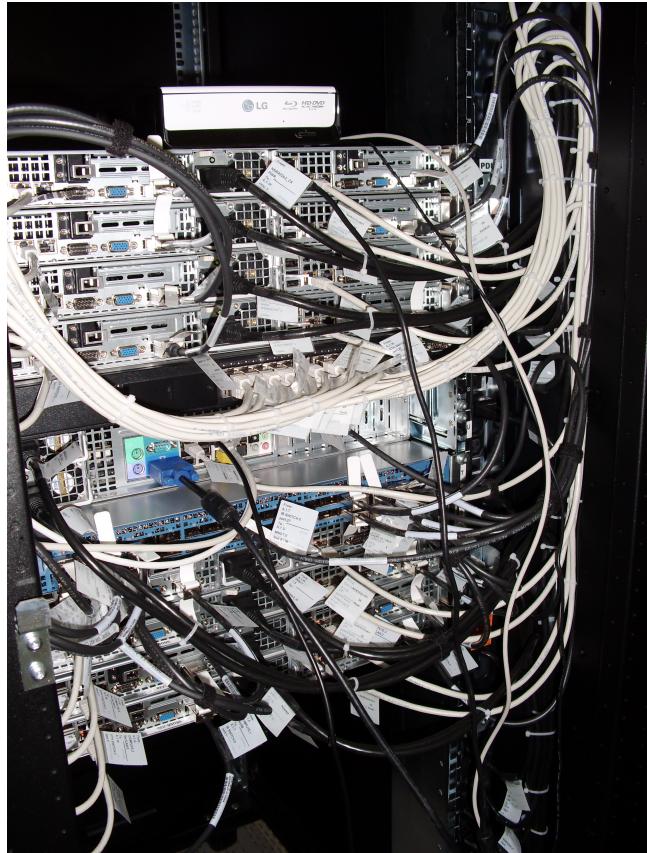
This is not Kramers, but related to another symmetry.

Q: tunneling gap for all s .

RESULT: very interesting behavior; there are some phonons that do not produce a tunneling gap thanks to the way they couple. SUSY at work.

(1) K. Irländer, H.-J. Schmidt, J. Schnack, Eur. Phys. J. B **94**, 68 (2021)

Summary



- Magnetic molecules for storage, q-bits, MCE, and since they are nice.
- SMM challenges: quantum tunneling and phonons
- Magnetism is much richer and more complicated than shown here. Talk focused on 3d ions with weak spin-orbit interaction.

Many thanks to my collaborators



- C. Beckmann, M. Czopnik, T. Glaser, O. Hanebaum, Chr. Heesing, M. Höck, K. Irländer, N.B. Ivanov, H.-T. Langwald, A. Müller, H. Schlüter, R. Schnalle, Chr. Schröder, J. Ummethum, P. Vorndamme (Bielefeld)
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Thank you very much for your
attention.

The end.

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