

Molecular Magnetism in High Magnetic Fields

Jürgen Schnack

Department of Physics – University of Bielefeld – Germany

4th International Symposium
on High Magnetic Field Spin Science in 100T
Sendai, Japan, November 26 - 28, 2007

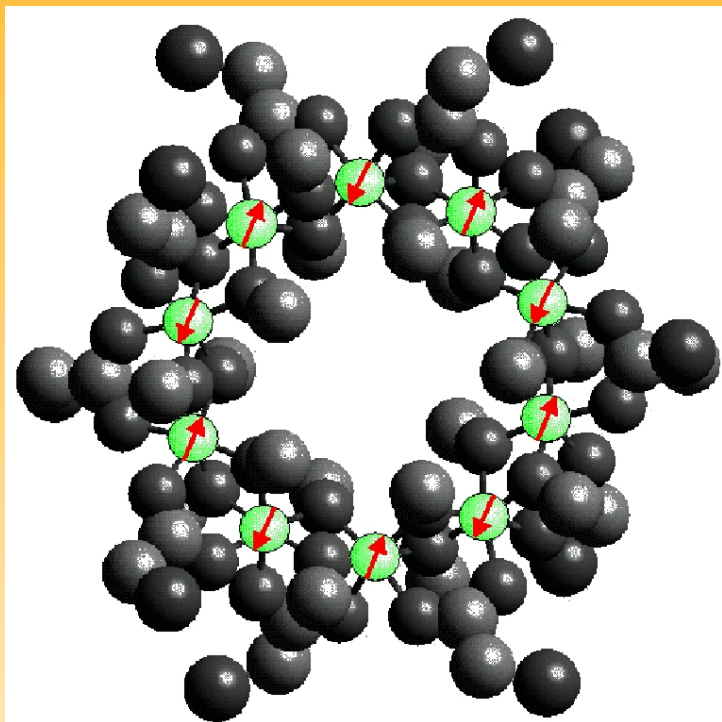


文部科学省

Many thanks to my collaborators worldwide

- T. Englisch, T. Glaser, S. Leiding, A. Müller, Chr. Schröder (Bielefeld)
- K. Bärwinkel, H.-J. Schmidt, M. Allalen, M. Brüger, D. Mentrup, D. Müter, M. Exler, P. Hage, F. Hesmer, K. Jahns, F. Ouchni, R. Schnalle, P. Shchelokovskyy, S. Torbrügge & M. Neumann, K. Küpper, M. Prinz (Osnabrück);
- M. Luban, D. Vaknin (Ames Lab, USA); P. Kögerler (RWTH, Jülich, Ames)
J. Musfeld (U. of Tennessee, USA); N. Dalal (Florida State, USA);
R.E.P. Winpenny (Man U, UK); L. Cronin (U. of Glasgow, UK);
H. Nojiri (Tohoku University, Japan); A. Postnikov (U. Metz)
- J. Richter, J. Schulenburg, R. Schmidt (U. Magdeburg);
S. Blügel (FZ Jülich); A. Honecker (U. Göttingen);
E. Rentschler (U. Mainz); U. Kortz (IUB); A. Tennant, B. Lake (HMI Berlin);
B. Büchner, V. Kataev, R. Klingeler, H.-H. Klauß (Dresden)

Contents for you today

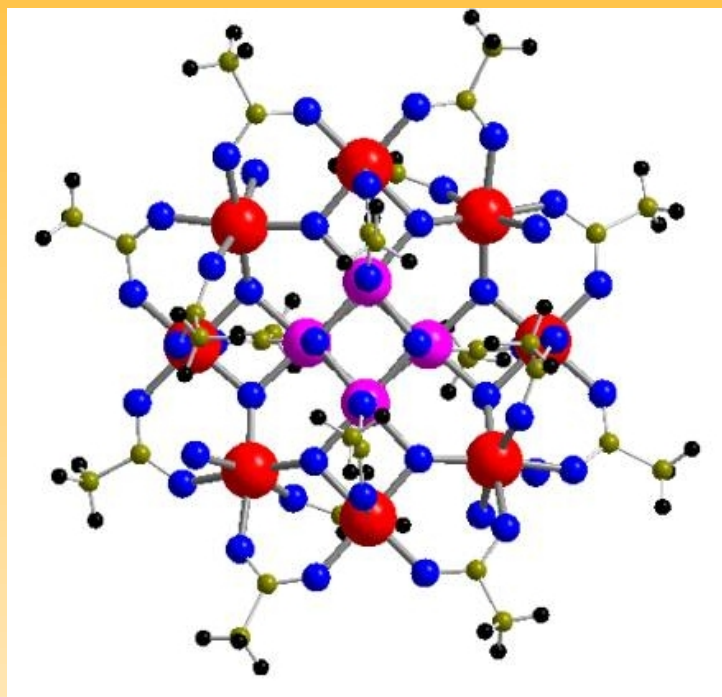


Fe₁₀

1. The suspects: magnetic molecules
2. Why high magnetic fields?
3. Fe₃₀ and friends
4. Metamagnetic phase transitions
5. Magnetostriction on the molecular level?

Magnetic Molecules

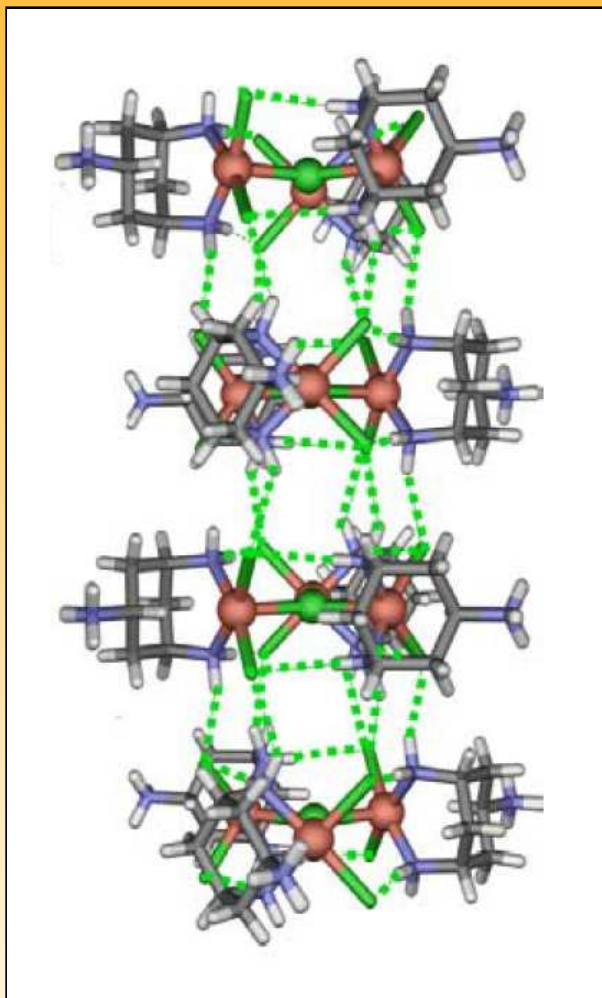
The beauty of magnetic molecules I



Mn₁₂

- Inorganic or organic macro molecules, where paramagnetic ions such as Iron (Fe), Chromium (Cr), Copper (Cu), Nickel (Ni), Vanadium (V), Manganese (Mn), or rare earth ions are embedded in a host matrix;
- Pure organic magnetic molecules: magnetic coupling between high spin units (e.g. free radicals);
- Speculative applications: magnetic storage devices, magnets in biological systems, light-induced nano switches, displays, catalysts, transparent magnets, qubits for quantum computers.

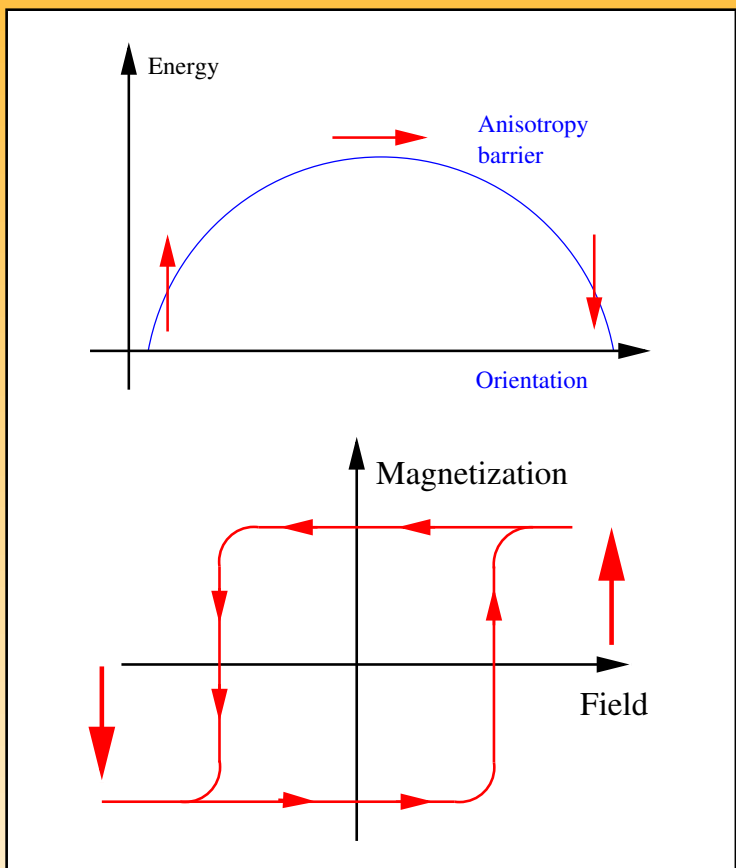
The beauty of magnetic molecules II



- Dimers (Fe_2), tetrahedra (Cr_4), cubes (Cr_8);
- Rings, especially iron and chromium rings
- Complex structures (Mn_{12}) – drosophila of molecular magnetism;
- “Soccer balls”, more precisely icosidodecahedra (Fe_{30}) and other macro molecules;
- Chain like and planar structures of interlinked magnetic molecules, e.g. triangular Cu chain:

J. Schnack, H. Nojiri, P. Kögerler, G. J. T. Cooper, L. Cronin, Phys. Rev. B 70, 174420 (2004); Sato, Sakai, Läuchli, Mila, ...

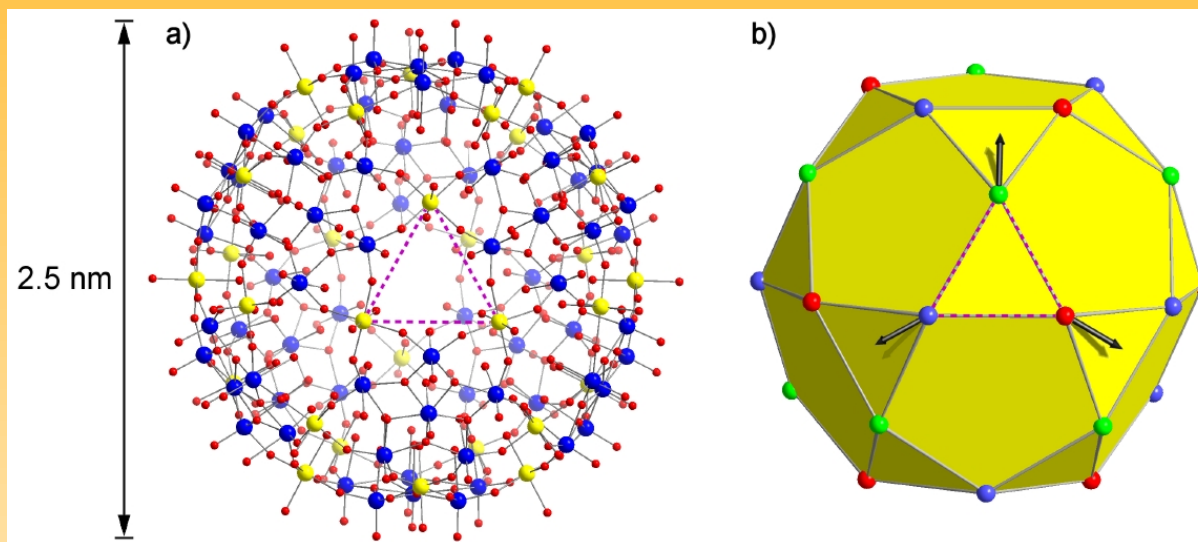
The beauty of magnetic molecules III



- Single Molecule Magnets (SMM): magnetic molecules with large ground state moment; e.g. $S = 10$ for Mn_{12} or Fe_8
- Anisotropy barrier dominates behavior (as in your hard drive);
- Single molecule is a magnet and shows metastable magnetization and hysteresis; but also magnetization tunneling.
- Today's major efforts: improve stability of magnetization; investigate on surfaces.

The beauty of magnetic molecules IV

{Mo₇₂Fe₃₀} – a giant magnetic Keplerate molecule

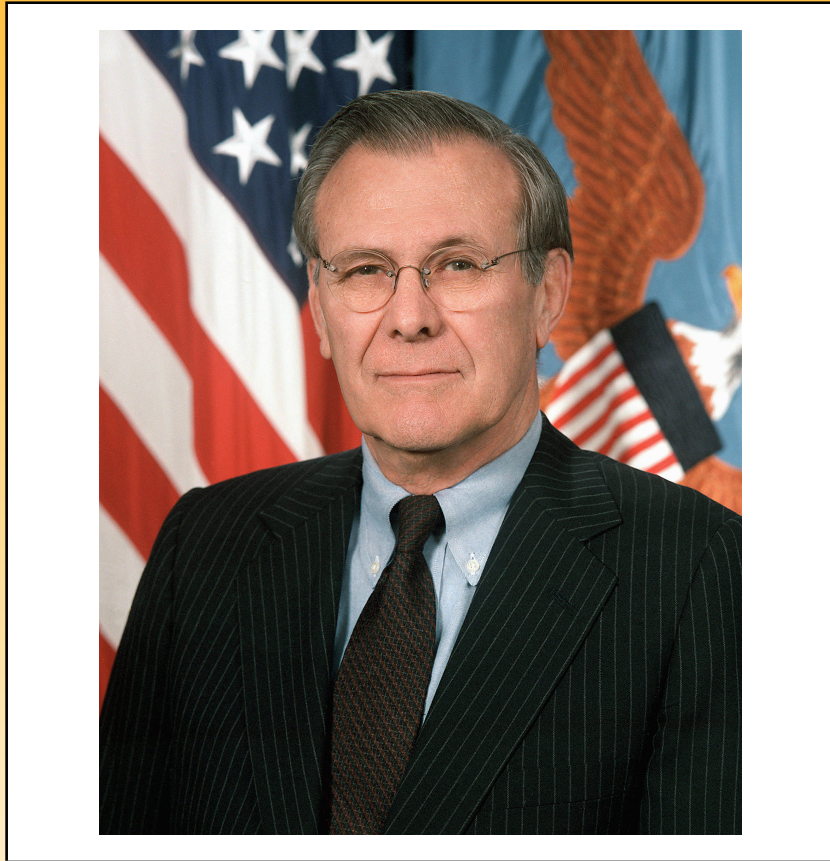


- Structure: Fe - yellow, Mo - blue, O - red;
- Exciting magnetic properties (1).
- Quantum treatment very complicated, dimension of Hilbert space $(2s + 1)^N \approx 10^{23}$ (2).

(1) A. Müller *et al.*, Chem. Phys. Chem. **2**, 517 (2001) , (2) M. Exler and J. Schnack, Phys. Rev. B **67**, 094440 (2003)

Why high magnetic fields?

Why high magnetic fields?

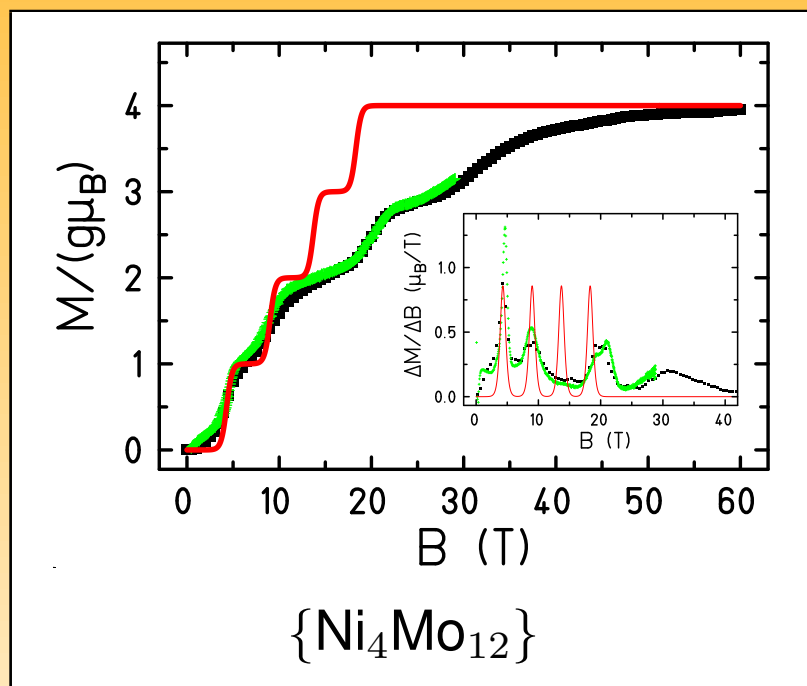


According to a recent philosopher:

- There are known knowns.
- There are known unknowns.
- And there are unknown unknowns.

Donald Rumsfeld

Why high magnetic fields? Because ...



- ...of the known unknowns and the unknown unknowns!
- Low-field susceptibility measurements, which in the field of molecular magnetism are often the sole measurements, do not yield a sufficient characterization of the material.
- You might miss essential features, especially for frustrated antiferromagnets, that only show up at high fields.

I will demonstrate this with three examples.

Model Hamiltonian – Heisenberg-Model

$$\tilde{H} = \sum_{i,j} \vec{\tilde{s}}(i) \cdot \mathbf{J}_{ij} \cdot \vec{\tilde{s}}(j) + \sum_{i,j} \vec{D}_{ij} \cdot [\vec{\tilde{s}}(i) \times \vec{\tilde{s}}(j)] + \mu_B B \sum_i^N g_i \tilde{s}_z(i)$$

Exchange/Anisotropy
Dzyaloshinskii-Moriya
Zeeman

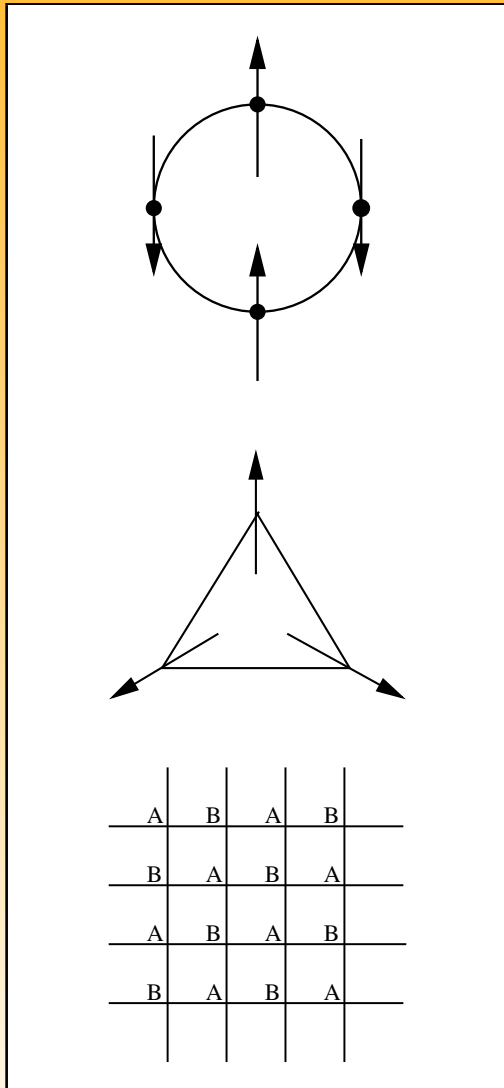
Very often anisotropic terms are utterly negligible, then ...

$$\tilde{H} = - \sum_{i,j} J_{ij} \vec{\tilde{s}}(i) \cdot \vec{\tilde{s}}(j) + g \mu_B B \sum_i^N \tilde{s}_z(i)$$

Heisenberg
Zeeman

The Heisenberg Hamilton operator together with a Zeeman term are used for the following considerations; $J < 0$: antiferromagnetic coupling.

Definition of frustration



- Simple: An antiferromagnet is frustrated if in the ground state of the corresponding classical spin system not all interactions can be minimized simultaneously.

- Advanced: A non-bipartite antiferromagnet is frustrated. A bipartite spin system can be decomposed into two sublattices A and B such that for all exchange couplings:

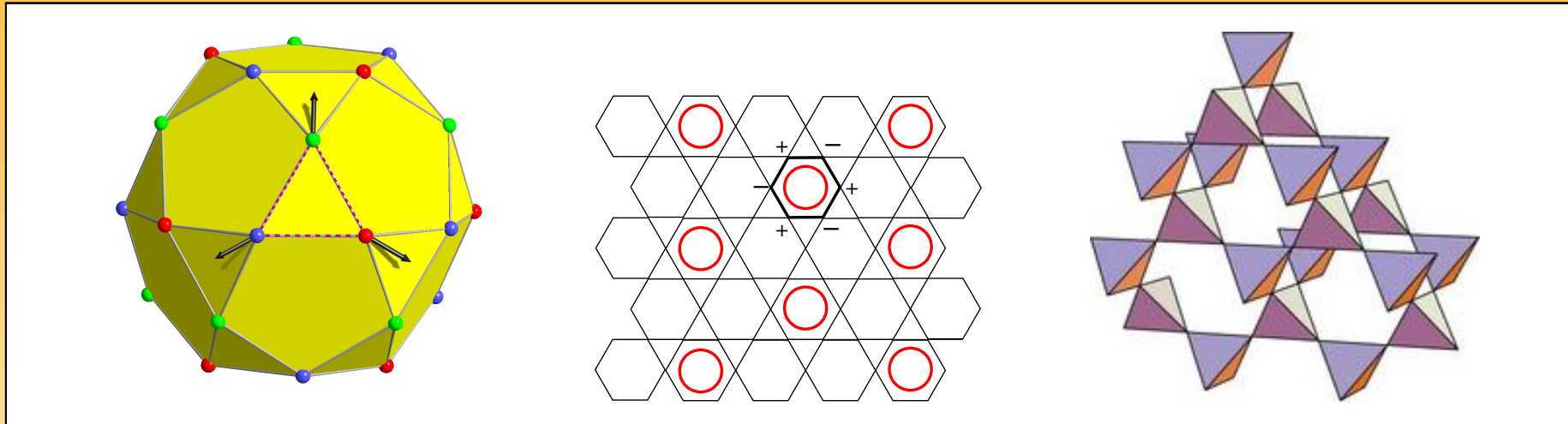
$$J(x_A, y_B) \leq g^2, J(x_A, y_A) \geq g^2, J(x_B, y_B) \geq g^2, \text{ cmp. (1,2).}$$

(1) E.H. Lieb, T.D. Schultz, and D.C. Mattis, Ann. Phys. (N.Y.) **16**, 407 (1961)
 (2) E.H. Lieb and D.C. Mattis, J. Math. Phys. **3**, 749 (1962)

Fe₃₀ and friends

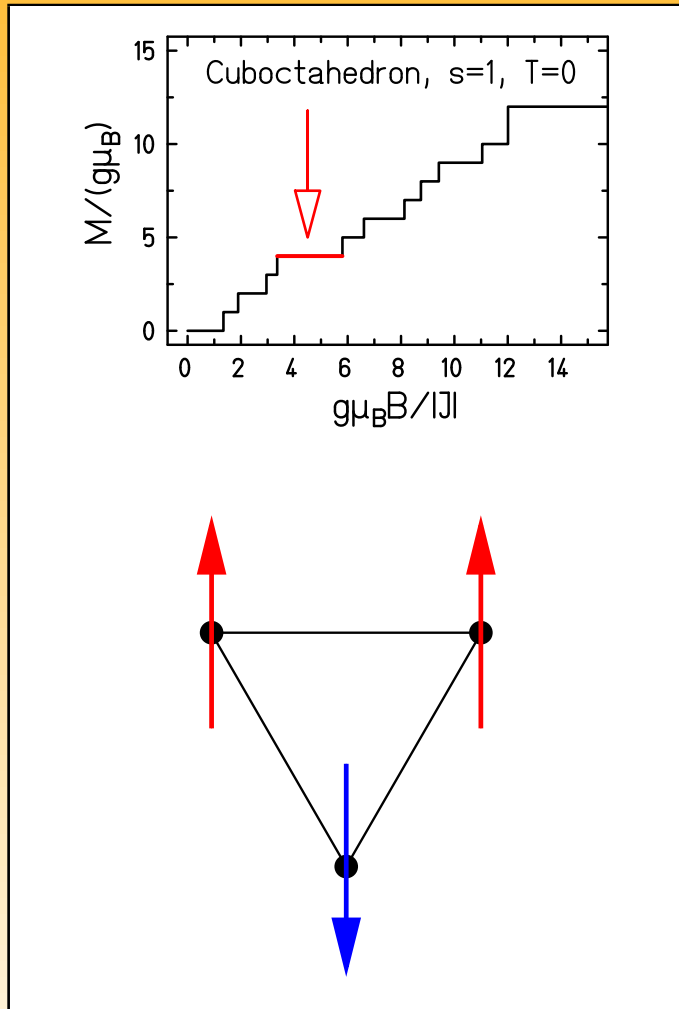
Fe₃₀ and friends

Corner sharing triangles and tetrahedra



- Several frustrated antiferromagnets show an unusual magnetization behavior, e.g. plateaus and jumps.
- Example systems: icosidodecahedron, kagome lattice, pyrochlore lattice.

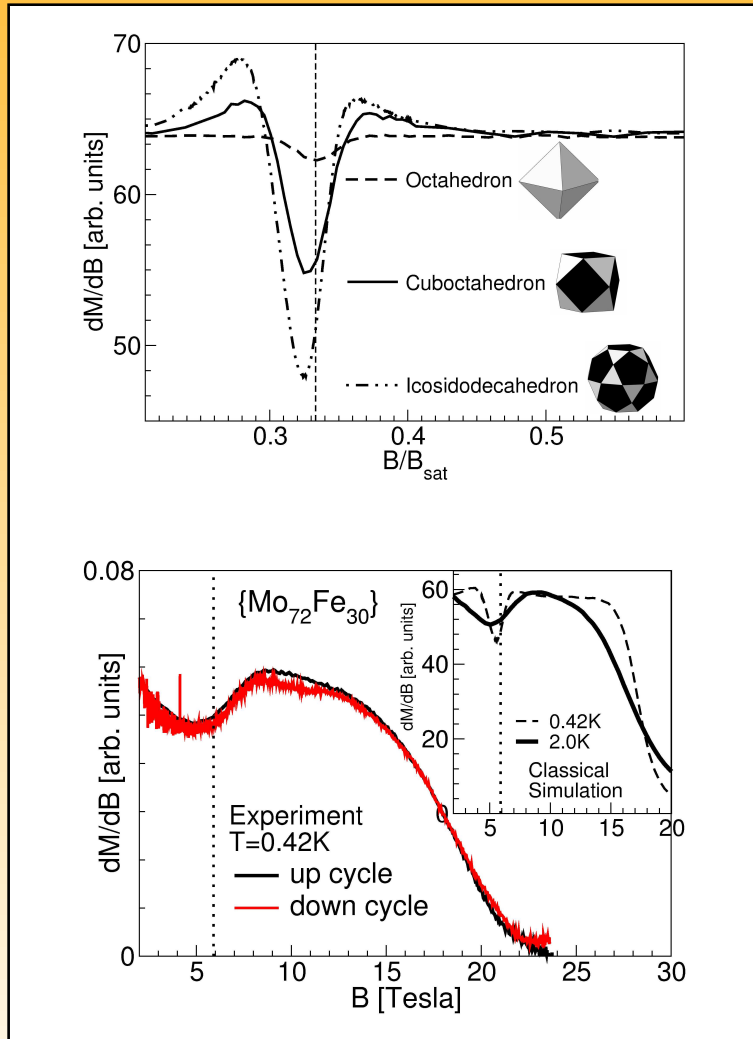
Magnetization plateaus and susceptibility minima



- Octahedron, Cuboctahedron, Icosidodecahedron: little (polytope) brothers of the kagome lattice with increasing frustration.
- Cuboctahedron & Icosidodecahedron realized as magnetic molecules.
- Cuboctahedron, Icosidodecahedron & kagome feature plateaus, e.g. at $\mathcal{M}_{\text{sat}}/3$.
- Plateau at $\mathcal{M}_{\text{sat}}/3$ due to **uud**-configuration. This configuration contributes substantially to the classical partition function; it is stabilized by quantum fluctuations.

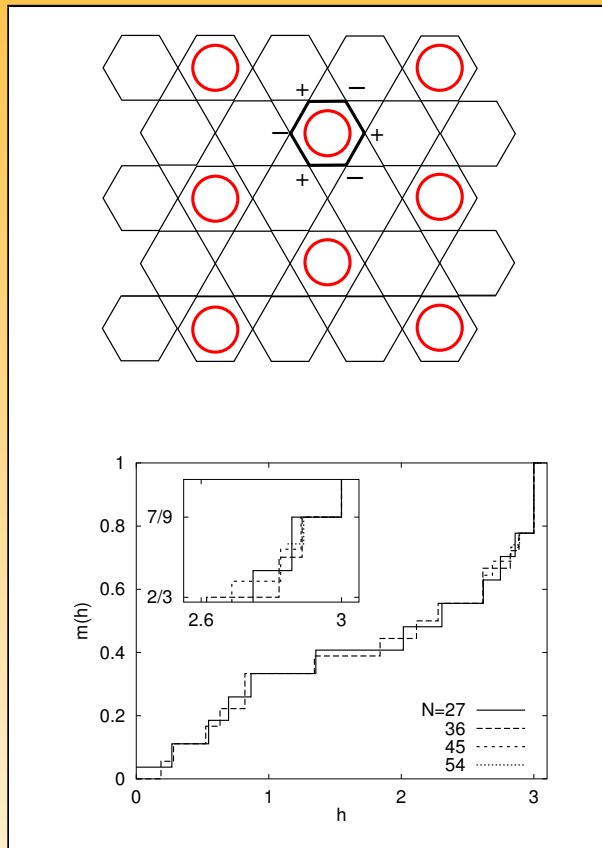
Recent comprehensive review by I. Rousochatzakis, A.M. Läuchli, F. Mila, arXiv:0711.3231v1

Magnetization plateaus and susceptibility minima



- Susceptibility shows a pronounced dip at $B_{sat}/3$ (classical calculations and quantum calculations for the cuboctahedron).
- Obvious in case of plateau at $\mathcal{M}_{sat}/3$, more subtle for other frustrated systems.
- Experimentally verified for $\{Mo_{72}Fe_{30}\}$.
C. Schröder, H. Nojiri, J. Schnack, P. Hage, M. Luban, P. Kögerler, Phys. Rev. Lett. **94**, 017205 (2005)
- Measurement reveals that couplings in Fe_{30} might be randomly distributed (unexpected unknown unknown!)

Giant magnetization jumps in frustrated antiferromagnets Kagome Lattice

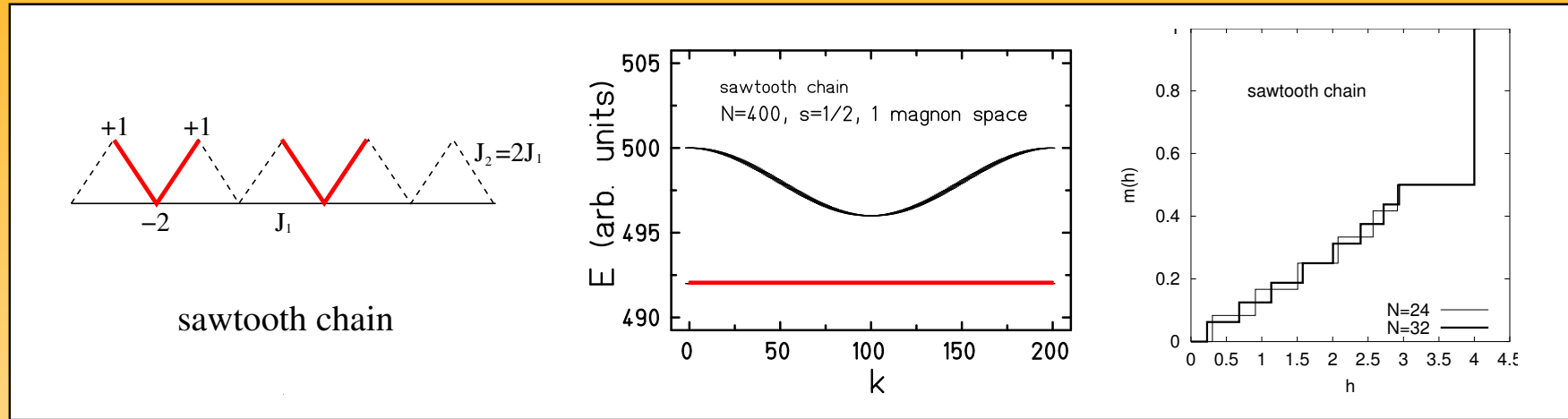


- Non-interacting one-magnon states can be placed on various lattices, e. g. kagome or pyrochlore;
- Each state of n independent magnons is the ground state in the Hilbert subspace with $M = Ns - n$;
Kagome: max. number of indep. magnons is $N/9$;
- Linear dependence of E_{\min} on M
 $\Rightarrow (T = 0)$ magnetization jump;
- Jump is a macroscopic quantum effect!
- A rare example of analytically known many-body states!

J. Schulenburg, A. Honecker, J. Schnack, J. Richter, H.-J. Schmidt, Phys. Rev. Lett. **88**, 167207 (2002)

J. Richter, J. Schulenburg, A. Honecker, J. Schnack, H.-J. Schmidt, J. Phys.: Condens. Matter **16**, S779 (2004)

Condensed matter physics point of view: Flat band

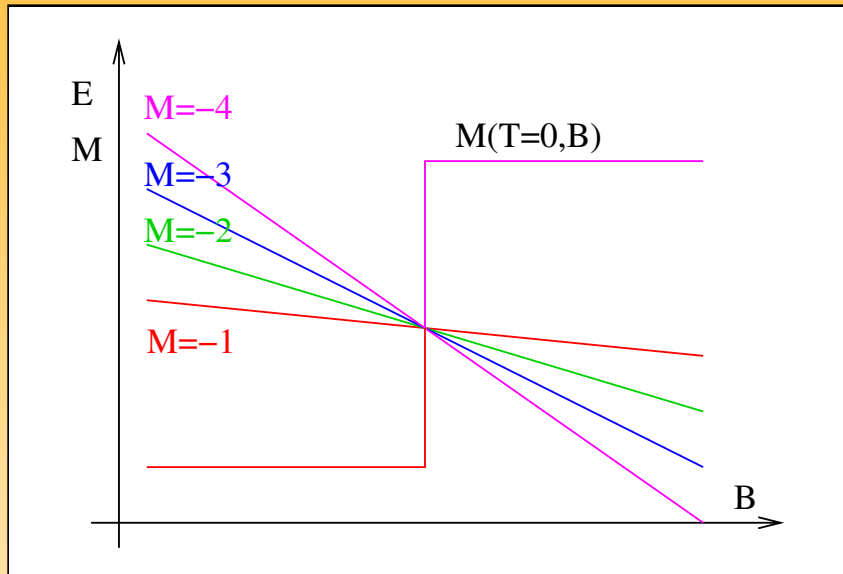


- Flat band of minimal energy in one-magnon space, i. e. high degeneracy of ground state energy in $\mathcal{H}(M = Ns - 1)$;
- Localized magnons can be built from those eigenstates of the translation operator, that belong to the flat band;
- There is a relation to flat band ferromagnetism (H. Tasaki & A. Mielke), compare (1).

(1) A. Honecker, J. Richter, Condens. Matter Phys. **8**, 813 (2005)

Magnetocaloric effect I

Giant jumps to saturation



- Many Zeeman levels cross at one and the same magnetic field.
- High degeneracy of ground state levels \Rightarrow large residual entropy at $T = 0$.

$$\left(\frac{\partial T}{\partial B}\right)_S = -\frac{T}{C} \left(\frac{\partial S}{\partial B}\right)_T$$

J. Schulenburg, A. Honecker, J. Schnack, J. Richter, H.-J. Schmidt, Phys. Rev. Lett. **88**, 167207 (2002)

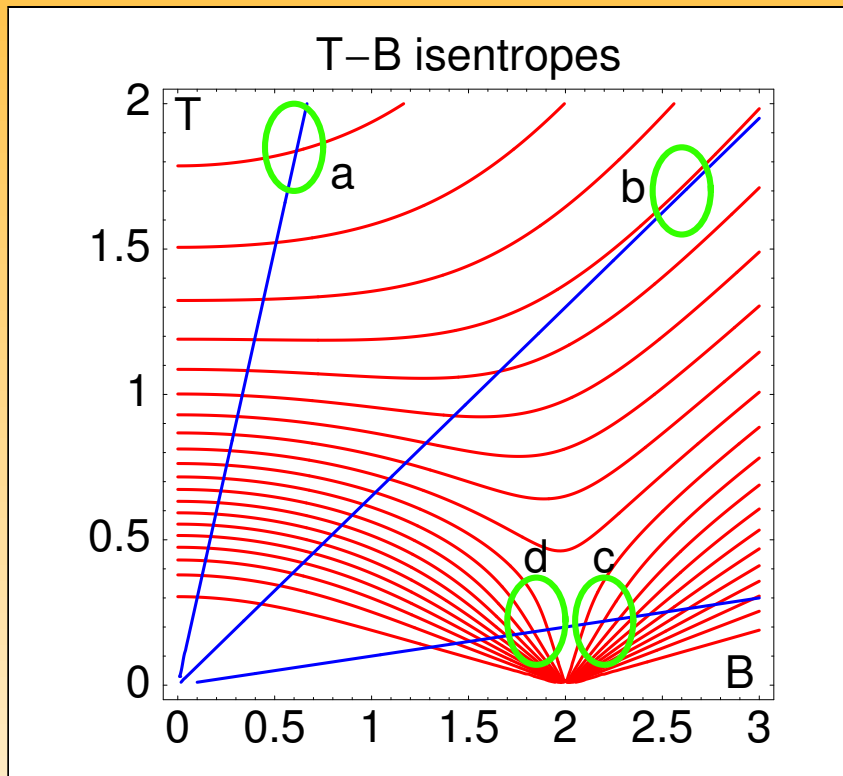
A. Honecker, J. Richter, Condensed Matter Physics **8**, 813 (2005)

H.-J. Schmidt, Johannes Richter, Roderich Moessner, J. Phys. A: Math. Gen. **39**, 10673 (2006)

O. Derzhko, J. Richter, A. Honecker, H.-J. Schmidt, Low Temp. Phys. **33**, 745 (2007)

Magnetocaloric effect II

Isentropes of an $s = 1/2$ dimer



blue lines: ideal paramagnet, red curves: af dimer

Magnetocaloric effect:

(a) reduced,

(b) the same,

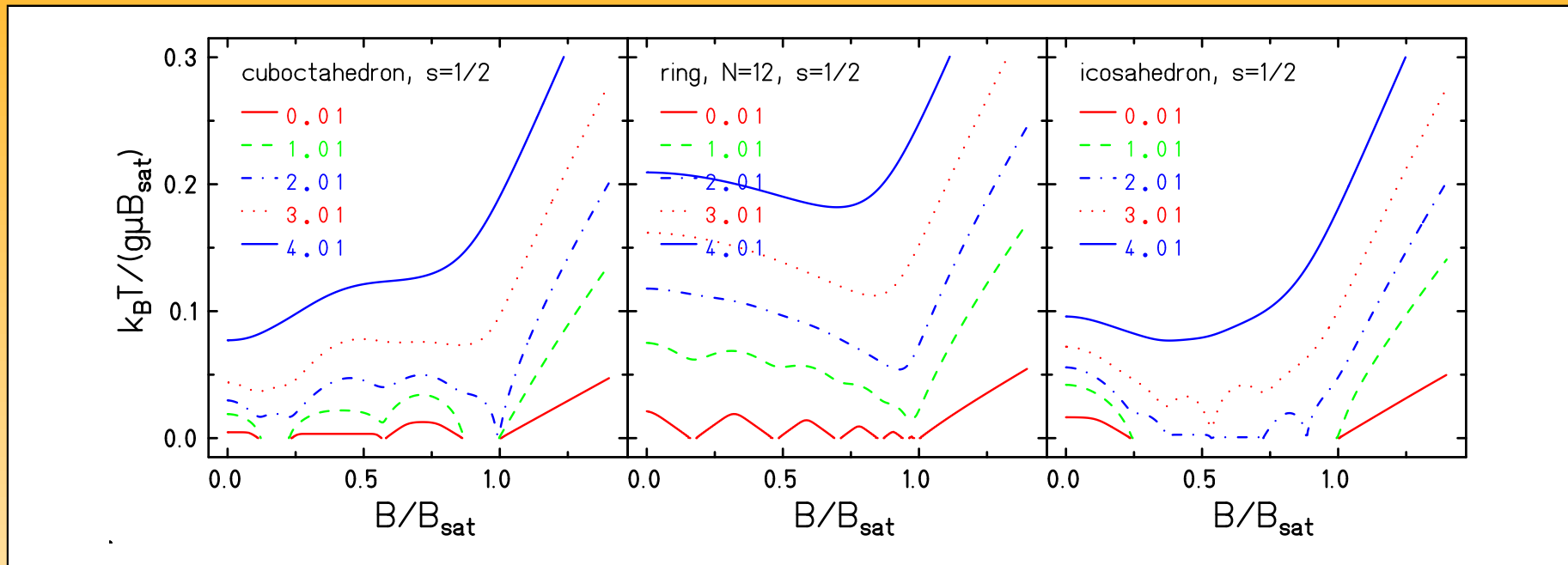
(c) enhanced,

(d) opposite

when compared to an ideal paramagnet.

Case (d) does not occur for a paramagnet.

Magnetocaloric effect III – Molecular systems



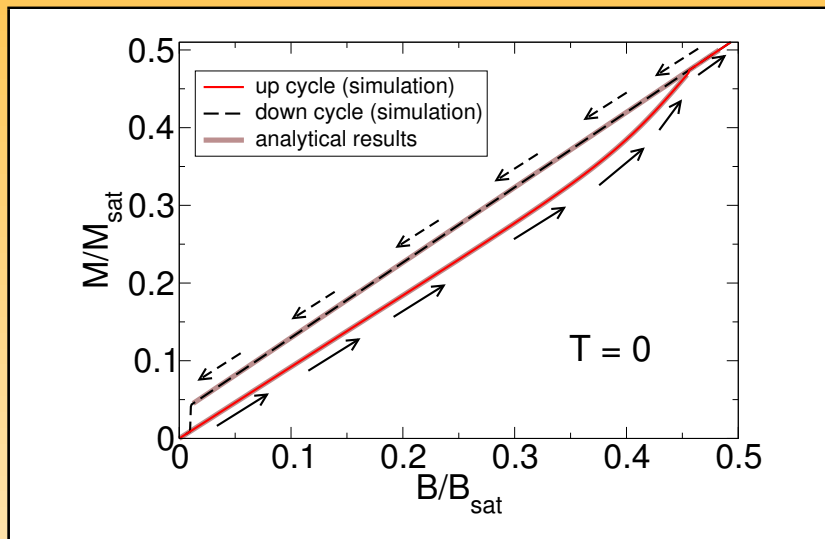
- Cuboctahedron: high cooling rate due to independent magnons;
- Ring: normal level crossing, normal jump;
- Icosahedron: unusual behavior due to edge-sharing triangles, high degeneracies all over the spectrum; high cooling rate.

J. Schnack, R. Schmidt, J. Richter, Phys. Rev. B **76**, 054413 (2007)

Metamagnetic phase transitions

Metamagnetic phase transition I

Hysteresis without anisotropy

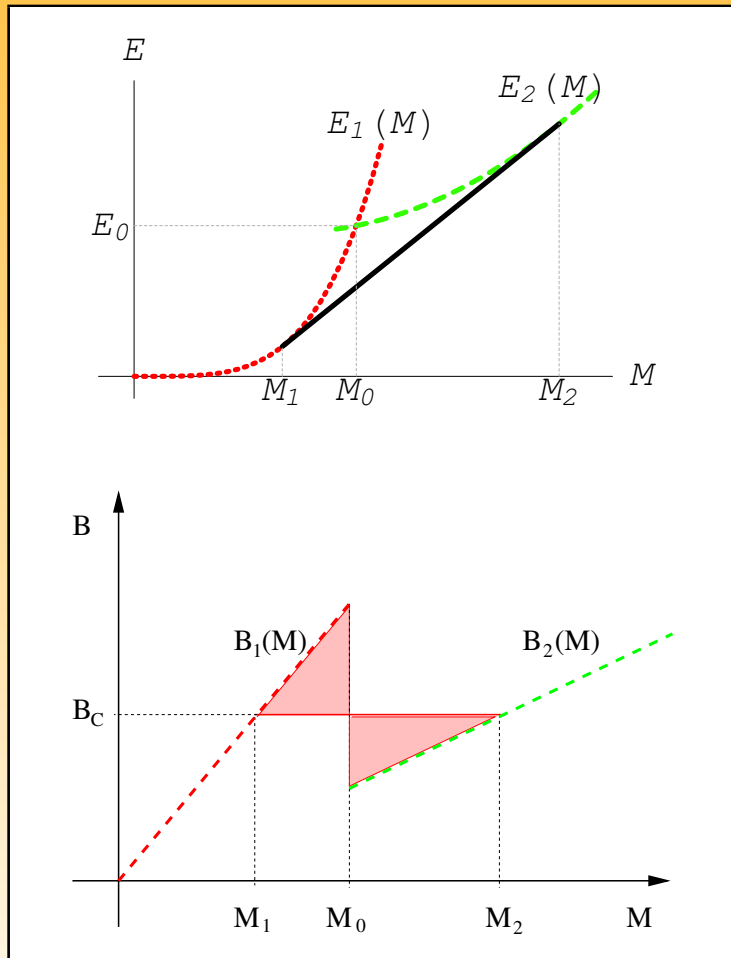


- Heisenberg model with isotropic nearest neighbor exchange
- Hysteresis behavior of the classical icosahedron in an applied magnetic field.
- Classical spin dynamics simulations (thick lines).
- Analytical stability analysis (grey lines).

C. Schröder, H.-J. Schmidt, J. Schnack, M. Luban, Phys. Rev. Lett. **94**, 207203 (2005)

Metamagnetic phase transition II

Non-convex minimal energy

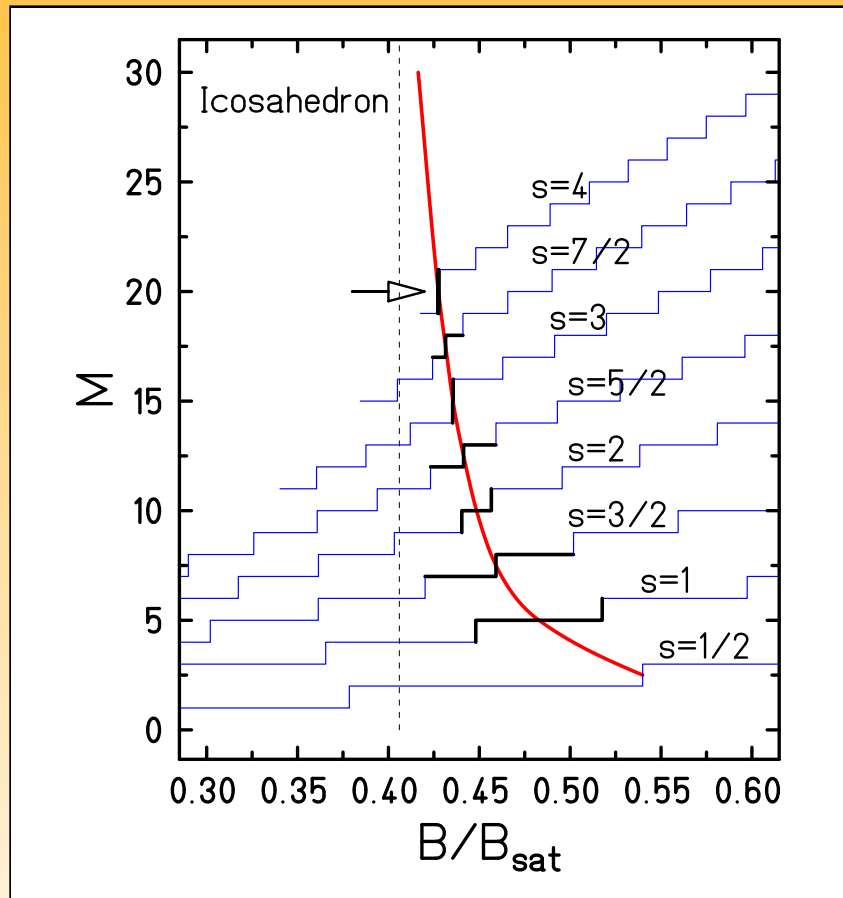


- Minimal energies realized by two families of spin configurations (1): $E_1(M)$ – “4- θ -family”, $E_2(M)$ – “decagon family”
- Overall minimal energy curve is not convex.
- Maxwell construction yields ($T = 0$) 1st order phase transition at B_c (1,2,3)
- ($T = 0$)–magnetization dynamics extends into metastable region.

(1) C. Schröder, H.-J. Schmidt, J. Schnack, M. Luban, Phys. Rev. Lett. **94**, 207203 (2005)
 (2) D. Coffey and S.A. Trugman, Phys. Rev. Lett. **69**, 176 (1992)
 (3) C. Lhuillier and G. Misguich, in *High Magnetic Fields*, Eds. C. Berthier, L. Levy, and G. Martinez, Springer (2002) 161-190

Metamagnetic phase transition III

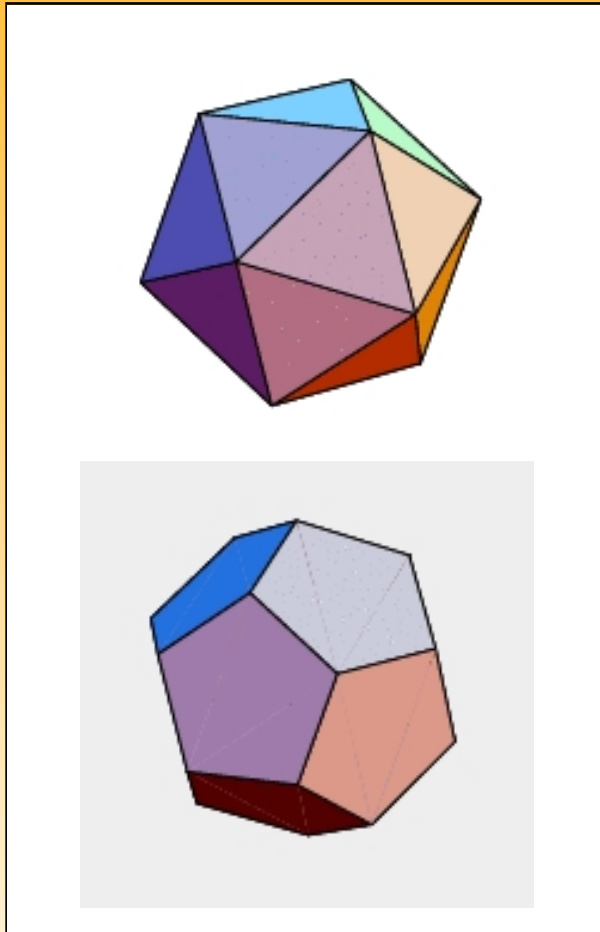
Quantum icosahedron



- Quantum analog:
Non-convex minimal energy levels
⇒ magnetization jump of $\Delta M > 1$.
- Lanczos diagonalization for various s .
- True jump of $\Delta M = 2$ for $s = 4$.
- Polynomial fit in $1/s$ yields the classically observed transition field.

C. Schröder, H.-J. Schmidt, J. Schnack, M. Luban,
Phys. Rev. Lett. **94**, 207203 (2005)

Similar transitions

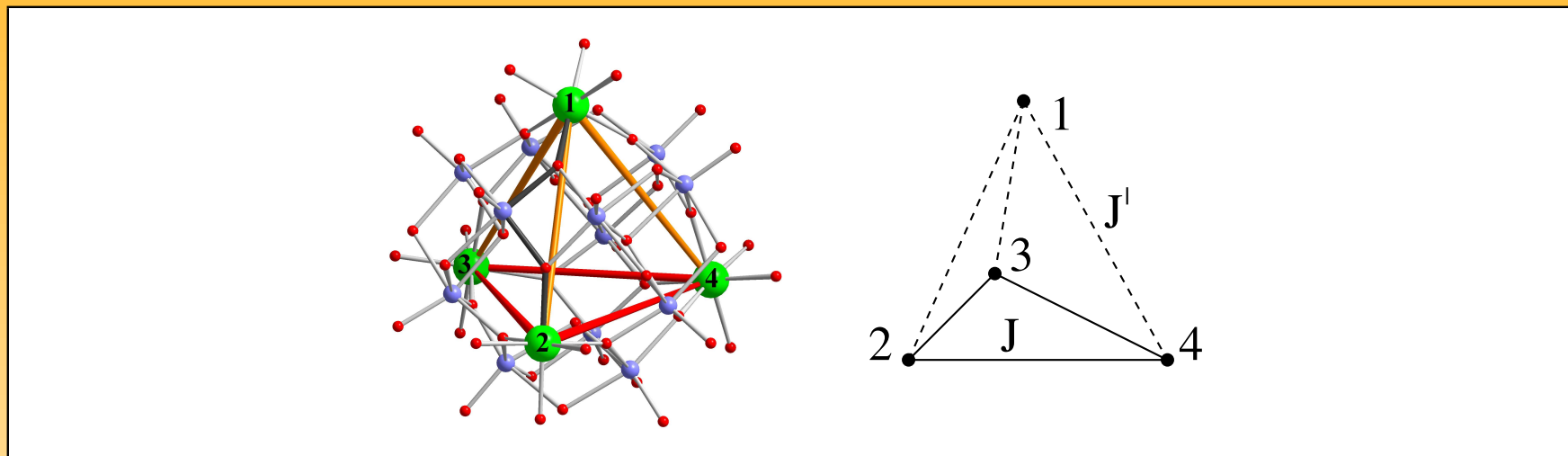


- First noticed in the context of the Buckminster fullerenes C_{20} and C_{60} (1).
- It seems to be important that the ground state is not coplanar and spins do not fold umbrella-like in field. The symmetry of low-field and high-field ground states needs to be different; Counter examples: $\{Mo_{72}Fe_{30}\}$, kagome lattice.
- This phase transition exists for many polytopes with **icosahedral symmetry**: numerical investigations for $20 \leq n \leq 720$ by N.P. Konstantinidis (2).

(1) D. Coffey and S.A. Trugman, Phys. Rev. Lett. **69**, 176 (1992).

(2) N.P. Konstantinidis, Phys. Rev. B **76**, 104434 (2007)

Magnetostriction on the molecular level?



- $[\text{Mo}_{12}^{\text{V}}\text{O}_{30}(\mu_2\text{-OH})_{10}\text{H}_2\{\text{Ni}^{\text{II}}(\text{H}_2\text{O})_3\}_4] = \{\text{Ni}_4\text{Mo}_{12}\}$ (1)
- Ni-Ni distances: $d_{12} = 6.700(5) \text{ \AA}$, $d_{13} = d_{14} = 6.689(1) \text{ \AA}$, $d_{23} = d_{24} = 6.616(1) \text{ \AA}$, $d_{34} = 6.604(1) \text{ \AA}$.
- Superexchange interactions J' and J represented by dashed and solid lines.

(1) A. Müller, C. Beugholt, P. Kögerler, H. Bögge, S. Bud'ko, and M. Luban, Inorg. Chem. **39**, 5176 (2000)

{Ni₄Mo₁₂}: naive expectations

Hamiltonian for almost perfectly tetrahedral symmetry and $s = 1$ (1)

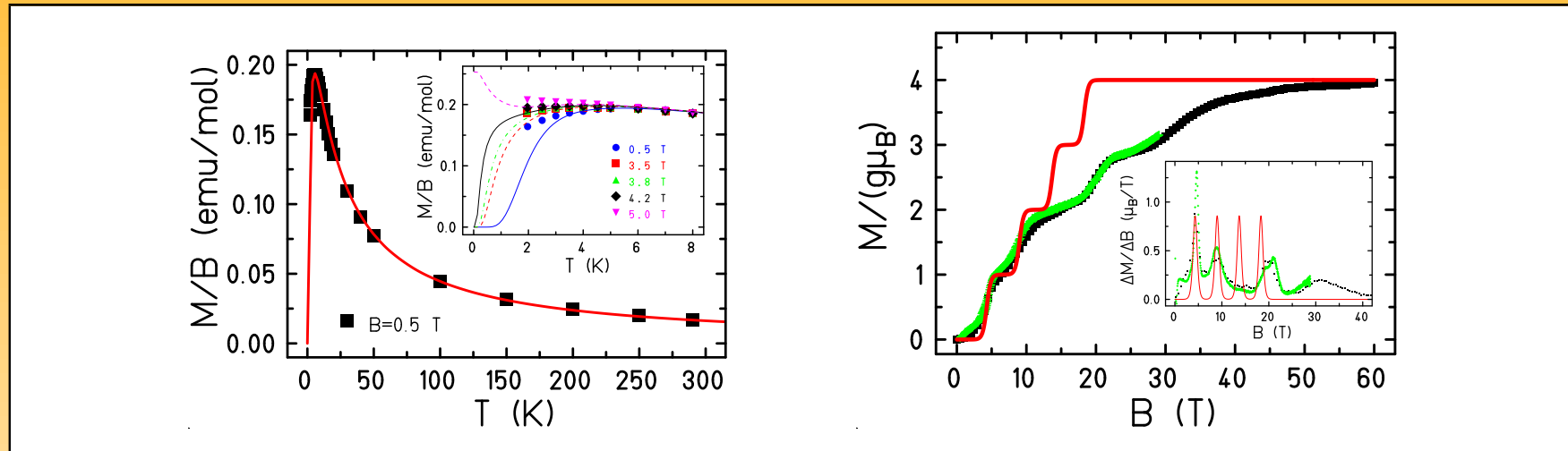
$$\tilde{H} = -2J \sum_{u < v} \tilde{\vec{s}}(u) \cdot \tilde{\vec{s}}(v) + g\mu_B \vec{B} \cdot \sum_u \tilde{\vec{s}}(u) = -J \left[\tilde{S}^2 - 4s(s+1) \right] + g\mu_B B \tilde{S}_z$$

Low-temperature magnetization curve $\mathcal{M}(B)$ should display four steps at

$$B_{S \rightarrow (S+1)} = -\frac{2J}{g\mu_B}(S+1)$$

(1) A. Müller, C. Beugholt, P. Kögerler, H. Bögge, S. Bud'ko, and M. Luban, Inorg. Chem. **39**, 5176 (2000)

{Ni₄Mo₁₂}: the reality



- Susceptibility reasonably well reproduced, finer details wrong.
- Magnetization deviates substantially: steps at 4.5, 8.9, 20.1, and 32 T.
- Use of two different exchange constants cannot account for the behavior.

Hamiltonian v.2007 (service pack II)

$$\underline{H} = \underline{H}_H + \underline{H}_{\text{ani}} + \underline{H}_{\text{biq-v.2007}} + \underline{H}_Z$$

Generalized biquadratic terms:

$$\underline{H}_{\text{biq-v.2007}} = - \sum_{t,u,v,w} j_{tuvw} \left(\underline{\vec{s}}(t) \cdot \underline{\vec{s}}(u) \right) \left(\underline{\vec{s}}(v) \cdot \underline{\vec{s}}(w) \right)$$

Original biquadratic terms: indices pairwise the same, i.e. $t = v$ & $u = w$.

(1) Norikiyo Uryû, S.A. Friedberg, *Phys. Rev.* **140**, A1803 (1965)

(2) V.V. Kostyuchenko, I.M. Markevtsev, A.V. Philippov, V.V. Platonov, V.D. Selemir, O.M. Tatsenko, A.K. Zvezdin, A. Caneschi, *Phys. Rev. B* **67**, 184412 (2003)

(3) V.V. Kostyuchenko, *Phys. Rev. B* (2007) accepted; M. Brüger, Ph.D. thesis, 2007

Interpretation

Interpretation of the generalized fourth-order terms:

- Higher order terms in the derivation of a spin Hamiltonian from the Hubbard model (1);
- Higher order terms in the derivation of a spin Hamiltonian from a spin-phonon Hamiltonian (2);
- Which scenario is valid? Maybe both!
- In the spin-phonon scenario the appearance of these terms means that the prefactors are not small. Since the prefactors are given by matrix elements of the Hesse matrix, this is equivalent to soft bonds! **MAGNETOSTRICTION!**
- These terms naturally lead to non-equidistant steps in the magnetization.

(1) V.V. Kostyuchenko *et al.*, Phys. Rev. B **67**, 184412 (2003)

(2) M. Brüger, Ph.D. thesis, 2007

I hope I could show you, that

There are interesting known knowns!

Models, Frustration, Magnetocalorics,

...

I hope I could show you, that

There are interesting known unknowns!

edge-sharing triangle-systems,

molecular magnetostriction, . . .

And I hope, that

**There are many more
unknown unknowns
to be discovered in high fields.**

The end is not in sight,
however, this talk is at its end!

Thank you very much for your attention.

German Molecular Magnetism Web

www.molmag.de

Highlights. Tutorials. Who is who. DFG SPP 1137