

# **Molecular Magnetism: Questions, Tools, and Answers**

Jürgen Schnack

Department of Physics – University of Bielefeld  
<http://obelix.physik.uni-bielefeld.de/~schnack/>

Seminar, Manchester Computing  
University of Manchester, July 11th 2007

## In late 20th century people coming from



transport theory



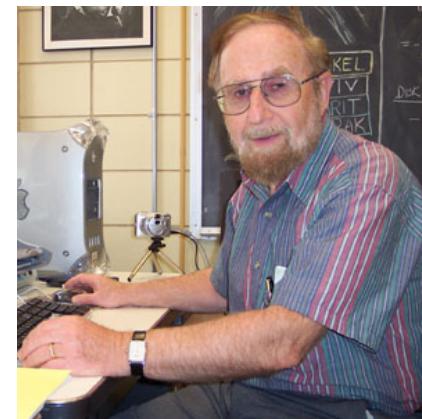
general relativity



nuclear physics



Schottky diodes

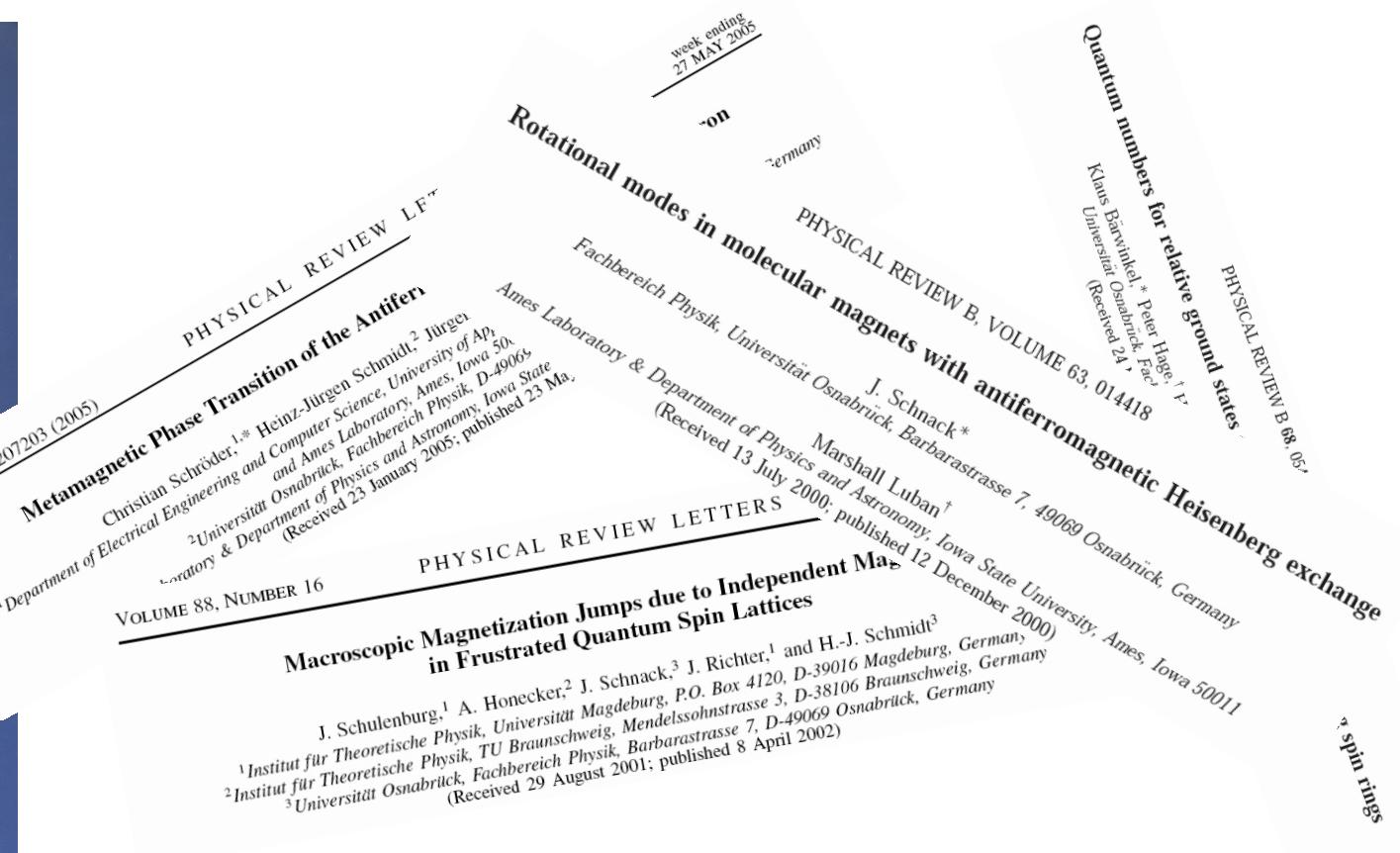
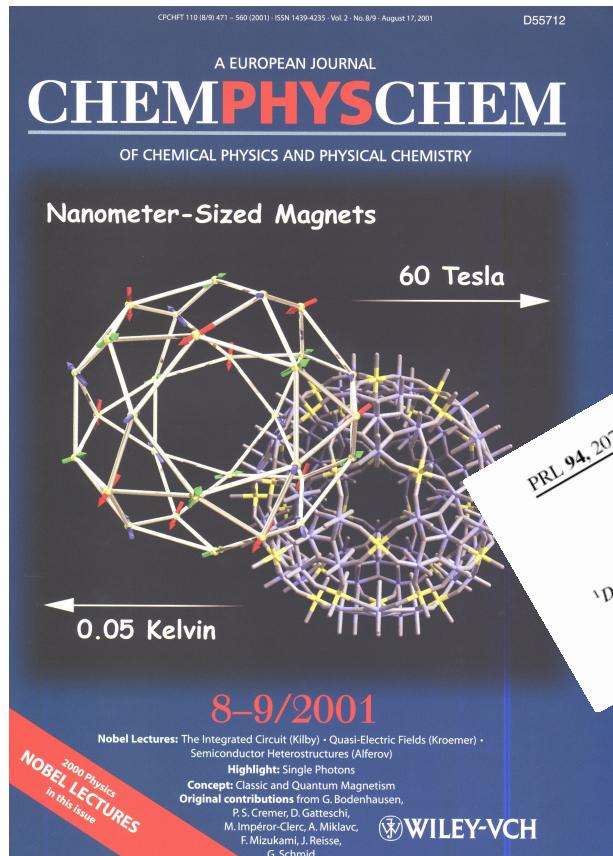


were triggered by a “magnetic” enthusiast.

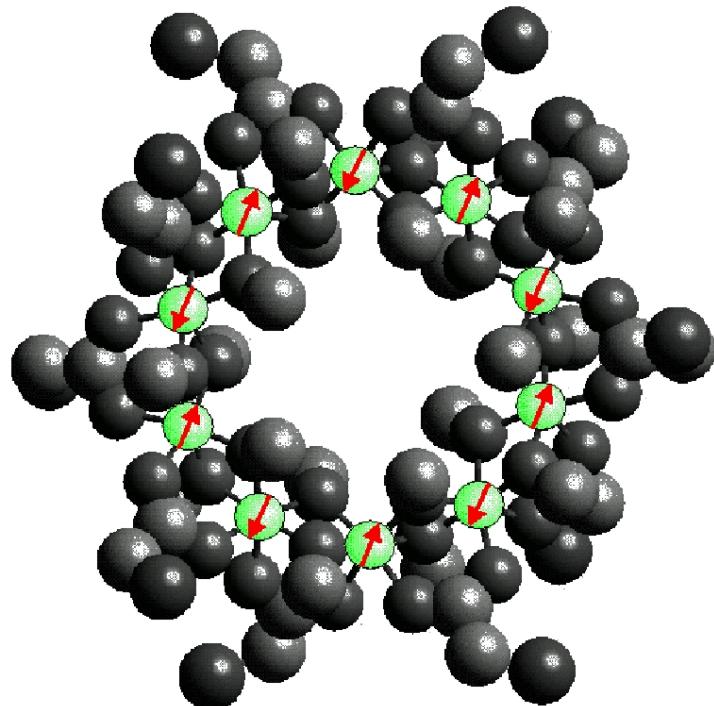
# Meanwhile a big collaboration has been established

- T. Englisch, T. Glaser, A. Müller (U. Bielefeld) & Chr. Schröder (FH Bielefeld);
- K. Bärwinkel, H.-J. Schmidt, M. Allalen, M. Brüger, D. Mentrup, D. Müter, M. Exler, P. Hage, F. Hesmer, K. Jahns, F. Ouchni, R. Schnalle, P. Shchelokovskyy, S. Torbrügge & M. Neumann, K. Küpper, M. Prinz (U. Osnabrück);
- M. Luban, D. Vaknin (Ames Lab, USA); P. Kögerler (RWTH, Jülich, Ames)  
J. Musfeld (U. of Tennessee, USA); N. Dalal (Florida State, USA);  
R.E.P. Winpenny (Man U, UK); L. Cronin (U. of Glasgow, UK);  
H. Nojiri (Tohoku University, Japan); A. Postnikov (U. Metz)
- J. Richter, J. Schulenburg, R. Schmidt (U. Magdeburg);  
S. Blügel (FZ Jülich); A. Honecker (U. Göttingen);  
E. Rentschler (U. Mainz); U. Kortz (IUB); A. Tennant, B. Lake (HMI Berlin);  
B. Büchner, V. Kataev, R. Klingeler (IFW Dresden)

# ... and various general results could be achieved



# Contents for you today

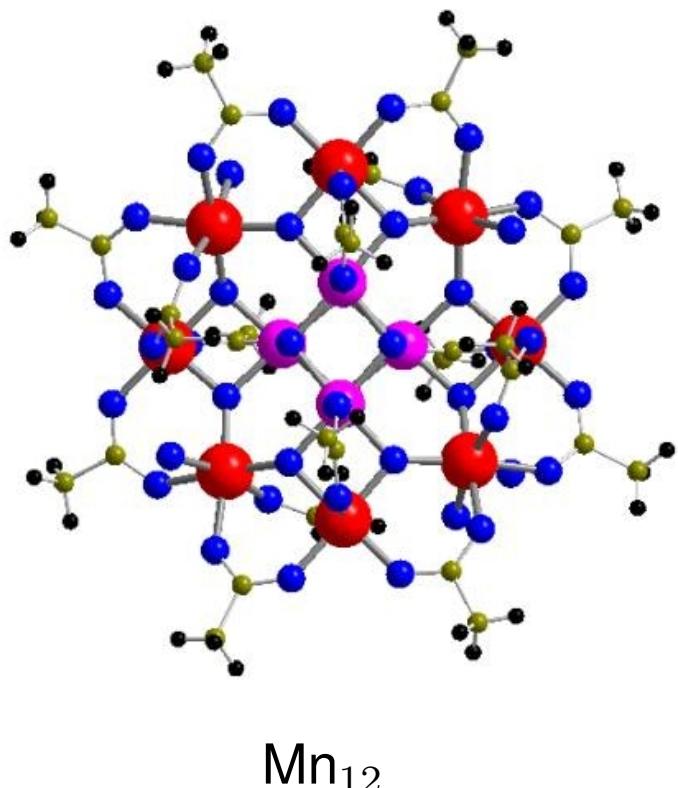


Fe<sub>10</sub>

1. The suspects: magnetic molecules
2. The thumbscrew: Heisenberg model
3. Giant magnetization jumps in frustrated antiferromagnets
4. Hysteresis without anisotropy
5. My hardware & parallelization issues

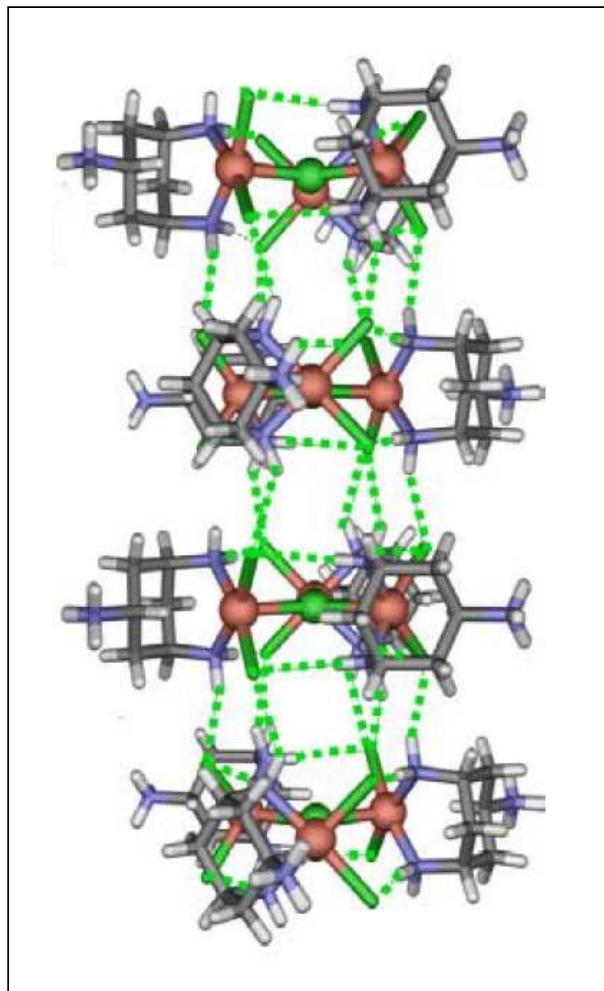
# Magnetic Molecules

# The beauty of magnetic molecules I



- Inorganic or organic macro molecules, where paramagnetic ions such as Iron (Fe), Chromium (Cr), Copper (Cu), Nickel (Ni), Vanadium (V), Manganese (Mn), or rare earth ions are embedded in a host matrix;
- Pure organic magnetic molecules: magnetic coupling between high spin units (e.g. free radicals);
- **Spin = magnetic moment (“compass needle”):** Molecule has magnetic properties.
- Speculative applications: **magnetic storage devices, magnets in biological systems, light-induced nano switches, displays, catalysts, transparent magnets, qubits for quantum computers.**

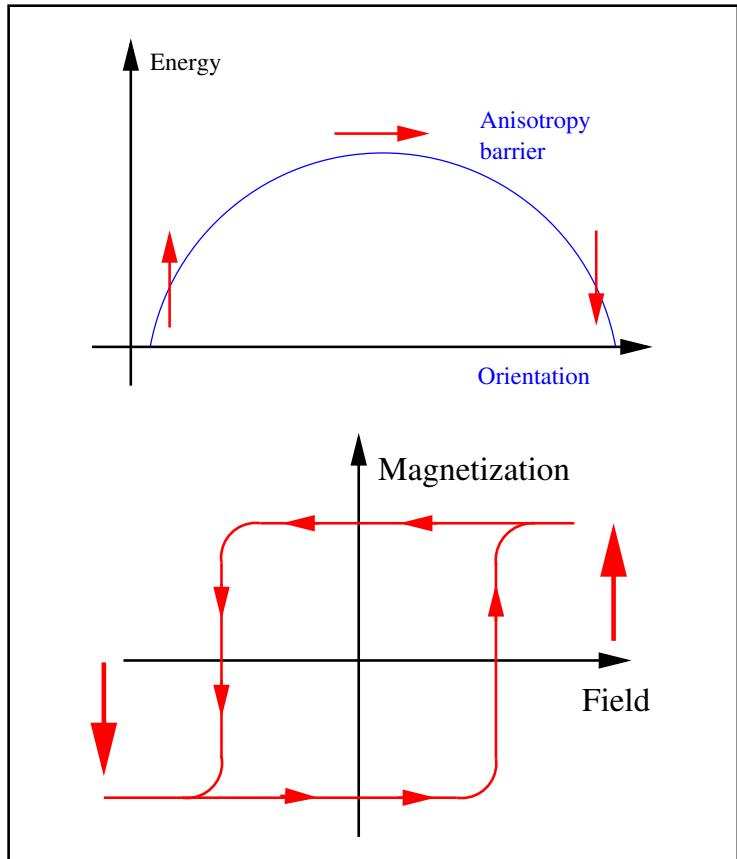
# The beauty of magnetic molecules II



- Dimers ( $\text{Fe}_2$ ), tetrahedra ( $\text{Cr}_4$ ), cubes ( $\text{Cr}_8$ );
- Rings, especially iron and chromium rings  
(order from [The Manchester Magic Ring Factory, Brunswick Street, Manchester, M13 9PL, UK](#));
- Complex structures ( $\text{Mn}_{12}$ ) – drosophila of molecular magnetism;
- “Soccer balls”, more precisely icosidodecahedra ( $\text{Fe}_{30}$ ) and other macro molecules;
- Chain like and planar structures of interlinked magnetic molecules, e.g. triangular Cu chain:

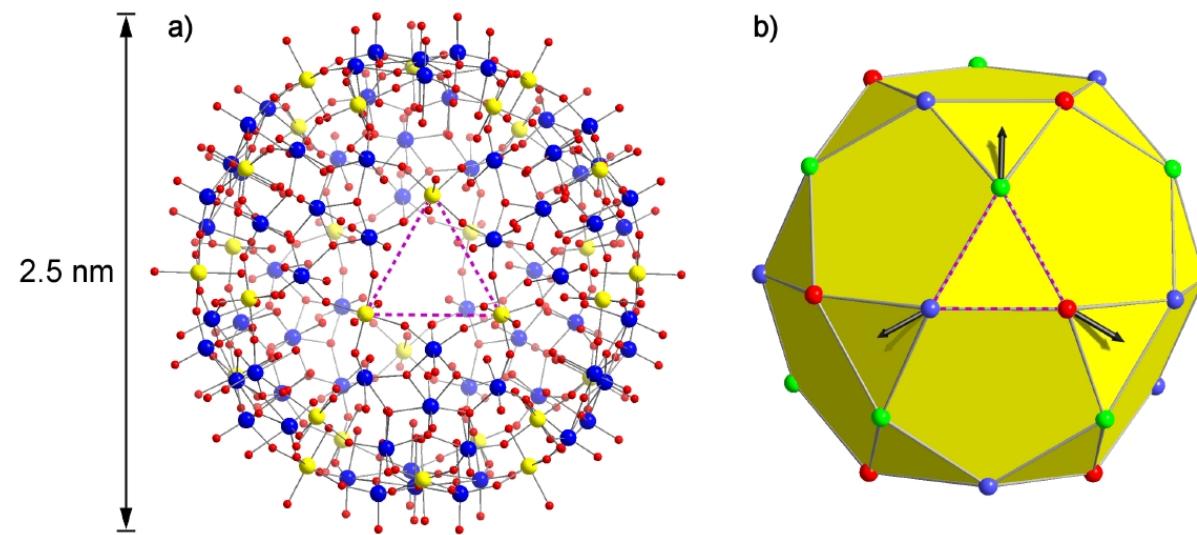
J. Schnack, H. Nojiri, P. Kögerler, G. J. T. Cooper, L. Cronin, Phys. Rev. B 70, 174420 (2004)

# The beauty of magnetic molecules III



- Single Molecule Magnets (SMM): magnetic molecules with large ground state moment; e.g.  $S = 10$  for  $\text{Mn}_{12}$  or  $\text{Fe}_8$
- Anisotropy barrier dominates behavior (as in your hard drive);
- Single molecule is a magnet and shows metastable magnetization and hysteresis; but also magnetization tunneling.
- Today's major efforts: improve stability of magnetization; investigate on surfaces.

# The beauty of magnetic molecules IV $\{\text{Mo}_{72}\text{Fe}_{30}\}$ – a giant magnetic Keplerate molecule



- Structure: Fe - yellow, Mo - blue, O - red;
- Exciting magnetic properties (1).
- Quantum treatment very complicated, dimension of Hilbert space  $(2s + 1)^N \approx 10^{23}$  (2).

(1) A. Müller *et al.*, Chem. Phys. Chem. **2**, 517 (2001) , (2) M. Exler and J. Schnack, Phys. Rev. B **67**, 094440 (2003)

# Numerics

# Model Hamiltonian – Heisenberg-Model

$$\tilde{H} = \sum_{i,j} \vec{s}(i) \cdot \mathbf{J}_{ij} \cdot \vec{s}(j) + \sum_{i,j} \vec{D}_{ij} \cdot [\vec{s}(i) \times \vec{s}(j)] + \mu_B B \sum_i^N g_i \tilde{s}_z(i)$$

Exchange/Anisotropy      Dzyaloshinskii-Moriya      Zeeman

Very often anisotropic terms are utterly negligible, then . . .

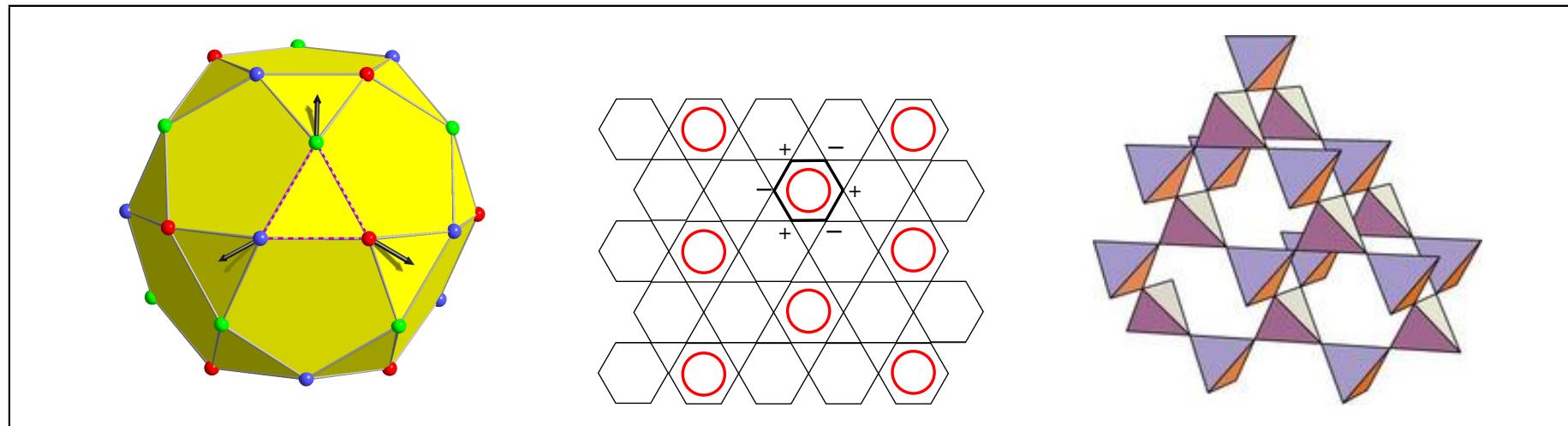
$$\tilde{H} = - \sum_{i,j} J_{ij} \vec{s}(i) \cdot \vec{s}(j) + g \mu_B B \sum_i^N \tilde{s}_z(i)$$

Heisenberg      Zeeman

The Hamilton operator is represented as a matrix whose eigenvalues and eigenvectors have to be computed. Maximum size  $\approx 30,000 \times 30,000$  complex\*16.

# Giant Magnetization Jumps

# Giant magnetization jumps in frustrated antiferromagnets I Systems



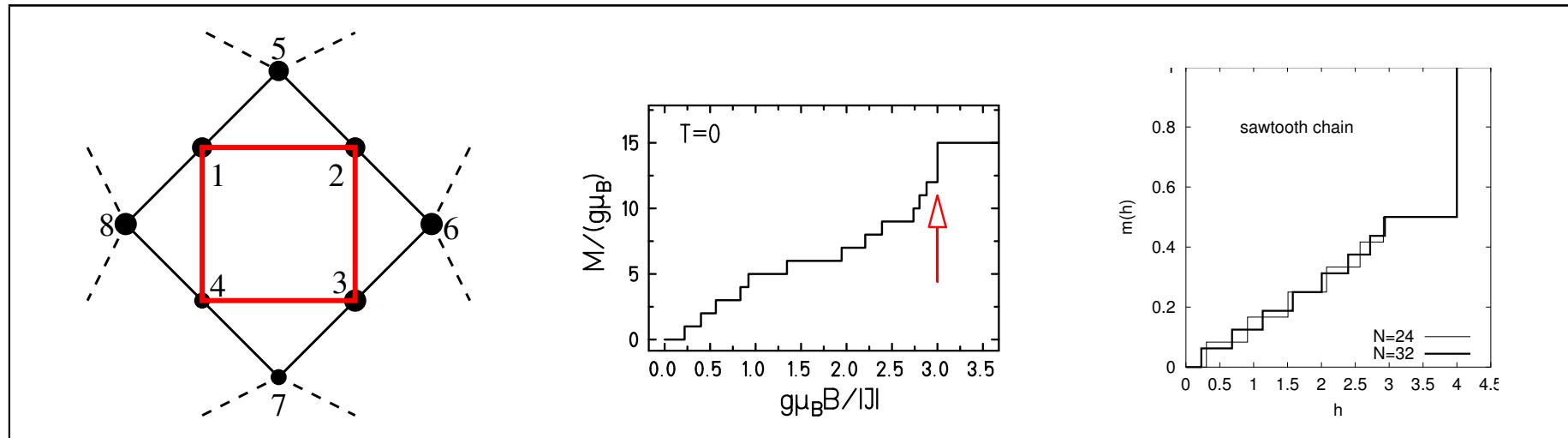
- Several frustrated antiferromagnets show an unusual behavior at the saturation field (1,2). AF =  $\uparrow\downarrow$ , saturation =  $\uparrow\uparrow\uparrow\uparrow\dots$
- Example systems: icosidodecahedron, kagome lattice, pyrochlore lattice.

(1) J. Schnack, H.-J. Schmidt, J. Richter, J. Schulenburg, Eur. Phys. J. B **24**, 475 (2001)

(2) J. Schulenburg, A. Honecker, J. Schnack, J. Richter, H.-J. Schmidt, Phys. Rev. Lett. **88**, 167207 (2002)

# Giant magnetization jumps in frustrated antiferromagnets II

## Magnetization jumps due to independent magnons

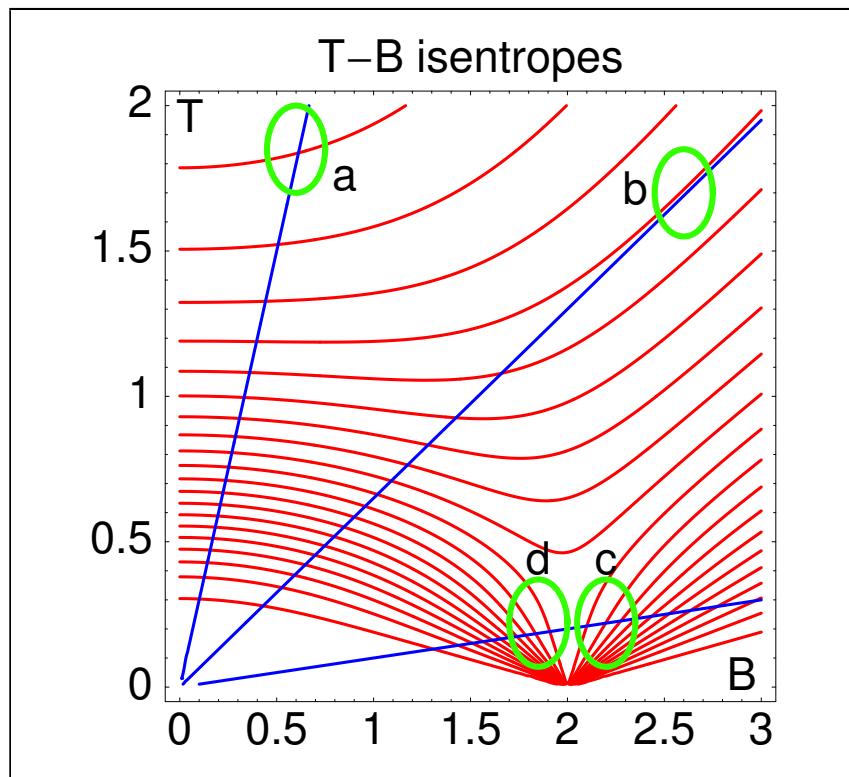


- Usually a magnetization curve is rather smooth.
- Unusually high magnetization jump at the saturation field.
- Many identical **localized independent magnons** flip their spins simultaneously.

J. Schulenburg, A. Honecker, J. Schnack, J. Richter, H.-J. Schmidt, Phys. Rev. Lett. **88**, 167207 (2002)  
 J. Richter, J. Schulenburg, A. Honecker, J. Schnack, H.-J. Schmidt, J. Phys.: Condens. Matter **16**, S779 (2004)

# Giant magnetization jumps in frustrated antiferromagnets III

## Giant magnetocaloric effect



blue lines: ideal paramagnet,  
red curves: af dimer

Magnetocaloric effect, i.e. temperature change when changing the applied magnetic field:

- (a) reduced,
- (b) the same,
- (c) enhanced,
- (d) opposite

when compared to an ideal paramagnet.

Case (d) does not occur for a paramagnet.

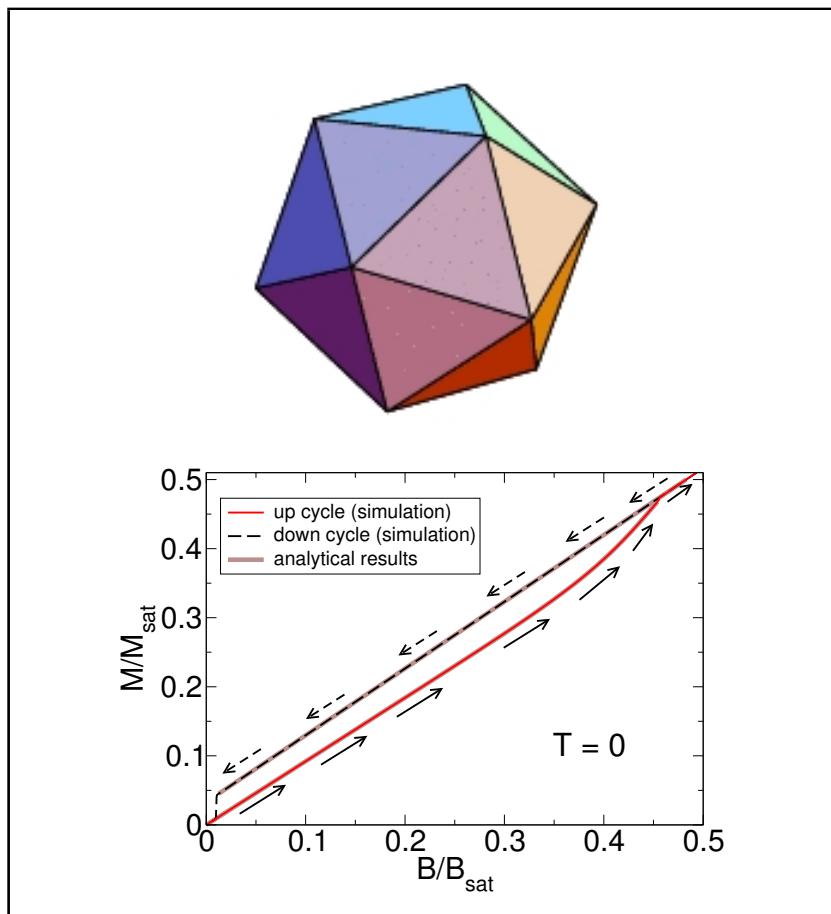
J. Schnack, J. Low Temp. Phys. **142** (2006) 279

J. Schnack, R. Schmidt, J. Richter, cond-mat/0703480

# Hysteresis without Anisotropy

# Metamagnetic phase transition I

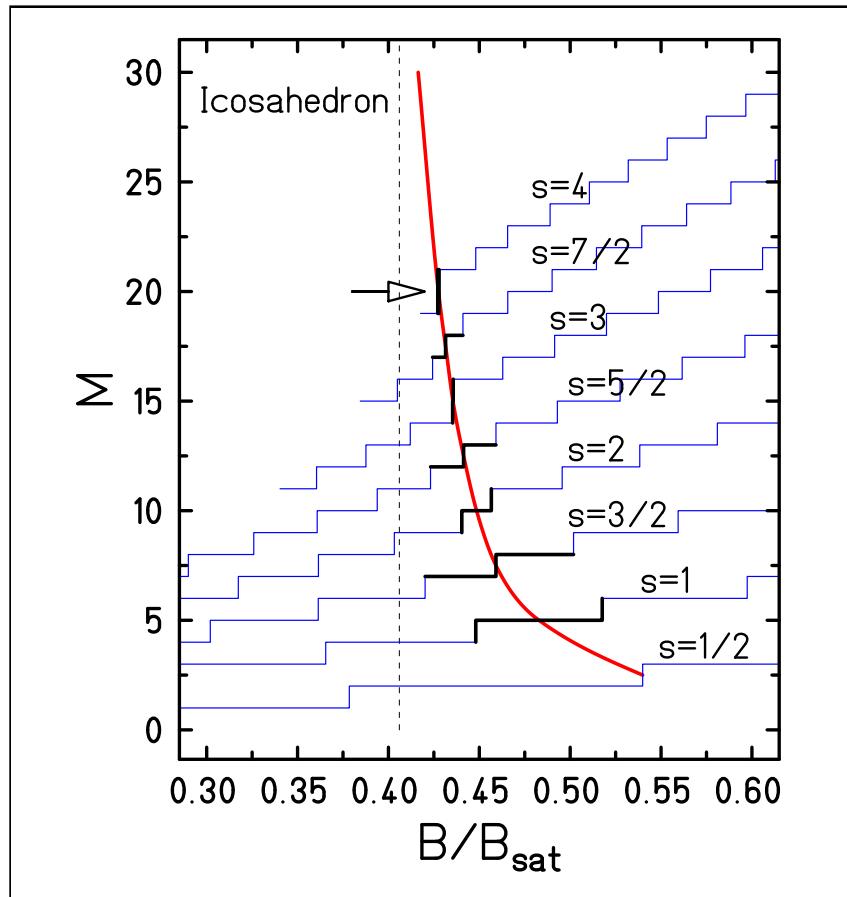
## Hysteresis without anisotropy



- Hysteresis is usually caused by anisotropy
- Hysteresis behavior of the classical isotropic Heisenberg icosahedron in an applied magnetic field.
- Classical spin dynamics simulations (thick lines + movie).
- Analytical stability analysis (grey lines).

C. Schröder, H.-J. Schmidt, J. Schnack, M. Luban, Phys. Rev. Lett. **94**, 207203 (2005)

# Metamagnetic phase transition II Quantum icosahedron



- Quantum analog:  
Non-convex minimal energy levels  
⇒ magnetization jump of  $\Delta M > 1$ .
- Lanczos diagonalization for various  $s$ .
- True jump of  $\Delta M = 2$  for  $s = 4$ .
- Polynomial fit in  $1/s$  yields the classically observed transition field.
- Numerics: Lanczos with vectors of lengths up to 1,342,275,012 used!

# My hardware & Parallelization issues

## Supercomputer 1st kind



Supercomputer  
1st kind  
(but . . .)

## Fuel not compatible with the Kyoto protocol



**2. Espresso**  
(Only 3 diagonalizations per gallon!)

## Supercomputer 2nd kind



- BULL NovaScale Server 3045:
- Future: wide open  
8 ITANIUM TUKWILA (a 4 cores),  
512 GB RAM  
(an amazing computer power)
- Now:  
4 ITANIUM MONTECITO (a 2 cores),  
64 GB RAM  
(already an amazing computer power,  
but one can get used to it ;-))

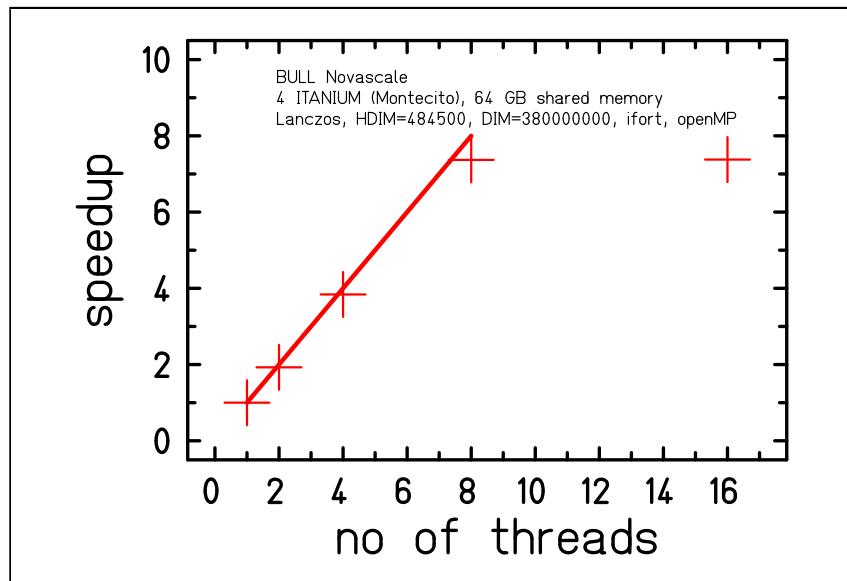
# Supercomputer 2nd kind

```
schnack@singlet:~/hpc
File Edit View Terminal Tabs Help
top - 15:50:00 up 35 min, 1 user, load average: 7.72, 7.82, 6.41
Tasks: 132 total, 9 running, 123 sleeping, 0 stopped, 0 zombie
Cpu0 : 100.0% us, 0.0% sy, 0.0% ni, 0.0% id, 0.0% wa, 0.0% hi, 0.0% si
Cpu1 : 100.0% us, 0.0% sy, 0.0% ni, 0.0% id, 0.0% wa, 0.0% hi, 0.0% si
Cpu2 : 100.0% us, 0.0% sy, 0.0% ni, 0.0% id, 0.0% wa, 0.0% hi, 0.0% si
Cpu3 : 100.0% us, 0.0% sy, 0.0% ni, 0.0% id, 0.0% wa, 0.0% hi, 0.0% si
Cpu4 : 100.0% us, 0.0% sy, 0.0% ni, 0.0% id, 0.0% wa, 0.0% hi, 0.0% si
Cpu5 : 100.0% us, 0.0% sy, 0.0% ni, 0.0% id, 0.0% wa, 0.0% hi, 0.0% si
Cpu6 : 100.0% us, 0.0% sy, 0.0% ni, 0.0% id, 0.0% wa, 0.0% hi, 0.0% si
Cpu7 : 100.0% us, 0.0% sy, 0.0% ni, 0.0% id, 0.0% wa, 0.0% hi, 0.0% si
Mem: 66751936k total, 9873792k used, 56878144k free, 142656k buffers
Swap: 2047872k total, 0k used, 2047872k free, 359040k cached

PID USER PR NI VIRT RES SHR S %CPU %MEM TIME+ COMMAND
5390 schnack 25 0 15.6g 8.5g 5952 R 99.9 13.4 24:53.33 glanczoshm-dode
5396 schnack 25 0 15.6g 8.5g 5952 R 99.9 13.4 24:37.46 glanczoshm-dode
5397 schnack 25 0 15.6g 8.5g 5952 R 99.9 13.4 24:52.95 glanczoshm-dode
5398 schnack 25 0 15.6g 8.5g 5952 R 99.9 13.4 24:57.60 glanczoshm-dode
5399 schnack 25 0 15.6g 8.5g 5952 R 99.9 13.4 25:39.64 glanczoshm-dode
5400 schnack 25 0 15.6g 8.5g 5952 R 99.9 13.4 25:10.02 glanczoshm-dode
5401 schnack 25 0 15.6g 8.5g 5952 R 99.9 13.4 25:39.93 glanczoshm-dode
5402 schnack 25 0 15.6g 8.5g 5952 R 99.9 13.4 25:09.29 glanczoshm-dode
1 root 15 0 5184 2880 2048 S 0.0 0.0 0:14.44 init
2 root RT 0 0 0 0 S 0.0 0.0 0:00.00 migration/0
```

# Parallelization issues I

**Improvement of Lanczos diagonalization for very large system size:**



- System size:  $10^{10} \dots 10^{12}$  entries per vector;
- Rearrangement of loops – outer loop writes (1);
- Evaluation of matrix elements “on the fly”, no storage;
- Analytical basis encoding in subspaces – faster than searching (1).

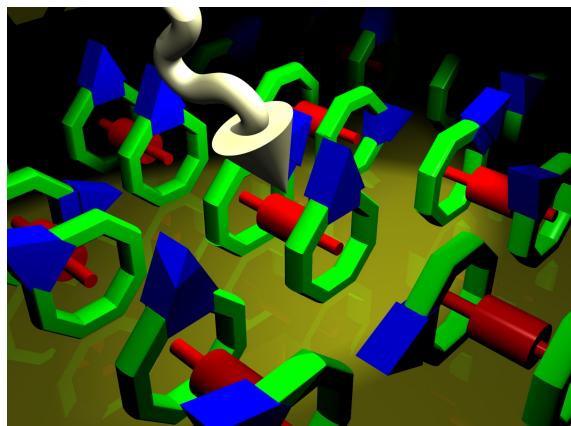
(1) J. Schnack, P. Hage, H.-J. Schmidt, arXiv:0706.3293v1 [cond-mat.str-el]



# Parallelization issues II

- **Goals:**  
Numerically exact treatment of small quantum systems;  
Ground states, spectroscopic data;  
Time evolution (including heat bath coupling)  
Thermodynamics, statistics.
- **Methodical problems:**  
openMP parallelization of exact diagonalization  
(INTEL currently improves MKL, Ben Bennett),  
openMP parallelization of approximate methods  
(Lanczos, Arnoldi, DMRG),  
Numerical accuracy of vectors with  $10^{10} \dots 10^{12}$  entries.

# Future HPC projects: The Manchester Gymwheel



- **Structure:**  
Two  $\text{Fe}_8$  rings glued together by 4 rungs;
- **Numerical demands:**  
Size of Hilbert space ( $s = 5/2$ ):  
 $(2s + 1)^N = 6^{16} = 2,821,109,907,456$   
Size of subspaces:  
 $\dim(\mathcal{H}(M = 0)) = 163,112,472,594$   
**If Manchester Computing hands over its BULL cluster, this might work!**
- **Workaround:**  
Use more symmetries or treat similar system with ( $s = 3/2$ ) instead.

## Summary

There is a big demand  
for fast and accurate numerics  
in the theory of magnetism.

And, the end is not in sight, . . .

... , however, this talk is at its end!

Thank you very much for your attention.

German Molecular Magnetism Web

[www.molmag.de](http://www.molmag.de)

Highlights. Tutorials. Who is who. DFG SPP 1137